ANALOG CIRCUITS LECTURE NOTES

(R22A0401)

B.TECH (II YEAR B.Tech – I SEM) (2024-25)

Prepared by: Dr. R. CHINNA RAO, Associate Professor Department of Electronics and Communication Engineering



DEPARTMENTOFELECTRONICS&COMMUNICATIONENGINEERING MALLAREDDYCOLLEGEOFENGINEERING&TECHNOLOGY

AutonomousInstitution–UGC,Govt.ofIndia

(AffiliatedtoJNTU,Hyderabad,ApprovedbyAICTE-AccreditedbyNBA&NAAC-'A'Grade-ISO9001:2008Certified) Maisammaguda,Dhulapally(PostViaHakimpet),Secunderabad–500100

MALLA REDDY COLLEGE OF ENGINEERING AND TECHNOLOGY

II Year B.Tech. ECE- I Sem

L/T/P/C 3/-/-/3

(R22A0401) ANALOG CIRCUITS

Course Objectives:

1. Learn the concepts of, load line analysis and biasing techniques

2. Learn the concepts of high frequency analysis of transistors.

3. To give understanding of various types of amplifier circuits

4. Learn the concepts of small signal analysis of BJT and FET amplifiers and biasing techniques

5. To familiarize the Concept of feedback in amplifiers so as to differentiate between negative and positive feedback. To design an oscillators at different frequencies.

UNIT – I

BJT Biasing: Transistor Biasing and Stabilization - Operating point, Need for biasing, DC Load line, Biasing - Fixed Bias, Self Bias, Bias Stability, Bias Compensation using Diode. Analysis of Small Signal Low Frequency BJT Amplifiers: Transistor Hybrid model, Analysis of single stage transistor amplifier using h-parameters: voltage gain, current gain, Input Impedance and Output impedance. Comparison of transistor configurations in terms of Ai, Ri,

Av ,and Ro.

UNIT –II

BJT Amplifiers-Frequency Response: Frequency response of an amplifier, Analysis at low and High Frequencies, Hybrid-pi (π) common emitter transistor model, Derive the hybrid- π model parameters, Millers theorem and it's dual. Multistage Amplifiers: Distortion in amplifiers, Analysis of cascaded BJT amplifier, Darlington pair and derive their input impedance(Ri) and current gain(Ai), coupling schemes-RC coupled amplifier, Transformer coupled amplifier, and Direct coupled Amplifier.

UNIT – III

FET-Biasing and FET Amplifiers: FET biasing: fixed bias and self bias. FET Amplifiers :Analysis of Common source (C.S), Common Drain (C.D) JFET Amplifiers, comparison of performance with BJT Amplifiers, Basic Concepts of MOSFET Amplifiers. **UNIT -IV**

FEEDBACK AMPLIFIERS: Concept of Feedback and types, Effects of negative feed back on amplifiers characteristics, voltage series, current series, current shunt, and voltage shunt feedback amplifiers.

UNIT -V

OSCILLATORS: Classification of oscillators, Barkhausen criterion, RC phase Shift

oscillator, Wien-bridge oscillator, LC oscillators- Hartley and Colpitts oscillator.

TEXT BOOKS:

1. Jacob Millman, Christos C Halkias -Integrated Electronics, McGraw Hill Education.

2. Robert L. Boylestead, Louis Nashelsky -Electronic Devices and

Circuits theory,11th Edition,2009, Pearson

REFERENCE BOOKS:

1. David A. Bell – Electronic Devices and Circuits, 5th Edition, Oxford.2. Adel S. Sedra, Kenneth C. Smith- Microelectronic Circuits-Theory and Applications, Oxford.

3. Chinmoy Saha, Arindam Halder, Debaati Ganguly -Basic Electronics-Principles and Applications,

Course Outcomes:

Upon completing this course, the students will be able to

1. Design the amplifiers with various biasing techniques.

- 2. Design single stage amplifiers using BJT and FET amplifier
- 3. Design multistage amplifiers and understand the concepts of High Frequency

Analysis of BJT.

4. Utilize the Concepts of negative feedback to improve the stability of Amplifiers and

Positive feedback to sustained oscillations and Analysis of oscillators at different frequencies

UNIT-1 TRANSISTOR BIASING AND STABILIZATION

NEED FOR TRANSISTOR BIASING

If the o/p signal must be a faithful reproduction of the i/p signal, the transistor must be operated in active region. That means an operating point has to be established in this region . To establish an operating point (proper values of collector current I_cand collector to emitter voltage V_{CE}) appropriate supply voltages and resistances must be suitably chosen in the ckt. This process of selecting proper supply voltages and resistance for obtaining desired operating point or Q point is called as biasing and the ckt used for transistor biasing is called as biasing ckt.

There are four conditions to be met by a transistors othat it acts as a faithful ampr:

- 1) Emitter base junction must be forward biased (V_{BE} =0.7Vfor Si, 0.2V for Ge) and collector base junction must be reverse biased for all levels of i/psignal.
- 2) V_{ce} voltage should not fall below $V_{CE(sat)}(0.3V$ for Si, 0.1V for Ge) for any part of the i/p signal. For V_{CE} less than $V_{CE(sat)}$ the collector base junction is not probably reverse biased.
- 3) The value of the signall_c when no signal is applied should beat least equal to the max.collector current t due to signal alone.
- 4) Max.rating of the transistorI_{c(max)},V_{CE(max)} andP_{D(max)} should not be exceed data any value ofi/p signal.

Consider the fig shown in fig 2.12. If operating point is selected at A,A representation condition when no bias is applied to the transistor i.e, $I_c=0$, $V_{CE}=0$. It does not satisfy the above said conditions necessary for faithful amplification.

Point C is too close to $P_{D(max)}$ curve of the transistor. Therefore the o/p voltage swing in the positive direction is limited.

Point B is located in the middle of active region .It will allow both positive and negative half cycles inthe o/psignal. It also provides linear gain and larger possible o/p voltages and currents

 ${\sf Hence} operating point for a transistor amplifier is selected to be in the middle of active region.$



Fig2.12CEOutputCharacteristics

DCLOADLINE

Referring to the biasing circuit of fig 2.13 a, the values of V_{CC} and R_{C} are fixed and Ic and V_{CE} are dependent on R_{B} .

 ${\sf Applying Kirchhoff's voltage law to the collector circuit in fig. 2.13, we get$



Fig2.13(a)CEAmplifie rCircuit (b)Load line

Vcc = IcRc + Vce

The straight line represented by ABinfig2.13b is called the dc load line. The coordinates of the end point A are obtained by substituting V_{CE}=0 in the above equation. Then $Ic = \frac{Vcc}{Rc}$. Therefore The coordinates of A areV_{CE}=0 and $Ic = \frac{Vcc}{Rc}$.

The coordinates of B are obtained by substituting Ic=0 in the above equation. Then Vce = Vcc. Therefore the coordinates of B are V_{CE} =Vcc and Ic=0. Thus the dc load line AB can be drawn if the values of Rc and Vcc are known.

As shown in the fig2.13b, the optimum POINT IS LOCATED AT THE MID POINT OF THE MIDWAY BETWEEN a AND b. In order to get faithful amplification, the Q point must be well within the active region of the transistor.

Even though the Q point is fixed properly, it is very important to ensure that the operating point remains stable where it is originally fixed. If the Q point shifts nearer to either A or B, the output voltage and current get clipped, thereby o/p signal is distorted.

In practice, the Q-point tends to shift its position due to any or all of the following three main factors.

- 1) Reverses a turation current, Ico, which doubles for every 10° Craise intemperature
- 2) Base emitter Voltage, VBE, which decreases by 2.5mVper°C
- 3) Transistor current gain, h_{FE} or β which in creases with temperature.

If base current I_B is kept constant since I_B is approximately equal to Vcc/RB. If the transistor is replaced by another one of the same type, one cannot ensure that the new transistor will have identical parameters as that o fthe first one. Parameters such as β vary over a range. This results in the variation of collector current Ic for a given I_B . Hence , in the o/p characteristics, the spacing between the curves might increase or decrease which leads to the shifting of the Q-point to a location which might be completely unsatisfactory.

ACLOADLINE

Afterdrawing the dc load line, the operating point Q is properly located at the centerofthe dc load line. This operating point is chosen under zero input signal condition of the circuit. Hence the ac load line should also pas through the operating point Q. The effective ac load resistance R_{ac} , is a combination of R_c parallelto R_{Li} . $R_{ac} = R_L || R_c$. So the slope of the ac load line CQD will $be\left(\frac{-1}{R_{ac}}\right)$. Todraw the ac load line, two end points, I.e. $V_{CE(max)}$ and $I_{C(max)}$ when the signal is applied are required.

 $V_{CE(\max)} = V_{CEQ + I_{CQ}}R_{ac}$, which locates point D on the Vce axis.

 $I_{c(\max)} = I_{CQ} + \frac{V_{CEQ}}{R_{ac}}$, which locates the point Con the I_caxis.

By joining point sc andD,aclo adlineCD is constructed. As R_C>R_{ac},The dc loadl ineis less steepthan ac load line.

STABILITYFACTOR(S):

The rise of temperature results in increase in the value of transistor gain β and the leakage current Ico. So, I_C also increases which results in a shift in operating point. Therefore, The biasing network should be provided with thermal stability. Maintenance of the operating point is specified by S,which indicates the degree of change in operating point due to change intemperature.

 $The extent to which {\sf I}_c is stabilized with varying {\sf I}_c is measured by a stability factor S$

$$S = \frac{\partial I_c}{\partial I_{co}} \approx \frac{dI_c}{dI_{co}} \approx \frac{\Delta I_c}{\Delta I_{co}}, \beta \text{ and } I_B \text{ constant}$$

For CEconfiguration $I_{C} = \beta I_{B} + (1 + \beta)I_{CO}$

Differentiatetheaboveequationw.r.tlc,Weget

$$1 = \beta \frac{dI_B}{dI_C} + (1+\beta) \frac{dI_{co}}{dI_c}$$
$$\therefore \quad \left(1 - \beta \frac{dI_B}{dI_C}\right) = \frac{(\beta+1)}{S}$$
$$\therefore \quad S = \frac{1+\beta}{1 - \beta \frac{dI_B}{dI_C}}$$

Sshouldbesmallto havebetterthermalstability.

StabilityfactorS'andS'':

S'isdefinedastherateofchangeofl_c with V_{BE} , keepingl_c and V_{BE} constant.

$$S' = \frac{\partial I_c}{\partial V_{BE}}$$

 $S'' is defined as the rate of change of I_C with \beta, keeping I_{CO} and V_{BE} constant.$

$$S'' = \frac{\partial I_c}{\partial \beta}$$

METHODS OF TRANSISTOR BIASING

1) Fixed bias(base bias)



Fig2.14FixedBiasing Circuit

Thisform of biasing is also called *basebias*. In the fig4.3 shown, the single powersource (for example, battery) is used for both collector and base of a transistor, although separate batteries can also be used.

Inthegivencircuit, V_{cc}

 $= I_BR_B + V_{be}$

Therefore, $I_B = (V_{cc} - V_{be})/R_B$

Since the equation is independent of current I_CR , $dI_B//dI_CR$ =0 and the stability factor is given by the equation..... reduces to

S=1+β

Sinceβisalargequantity,thisisverypoorbiasingcircuit.Thereforeinpractice thecircuitisnotusedfo biasing.

 $\label{eq:starses} For a given transistor, V_{be} does not vary significantly during use. As V_{cc} is offixed value, on selection of R the base current I_B is fixed. Therefore this type is called$ *fixed bias*type of circuit. Also for

given circuit, V_{cc}= I_CR_C+ V_{ce}

Therefore, V_{ce}=V_{cc}-I_CR_C

Merits:

• It is simplet oshift the operating point anywhere in the active region by merely changing the base resistor (R_B).

• Averysmallnumberofcomponents arerequired.

Demerits:

• The collector current does not remain constant with variation intemperature or power supply voltage. Therefore the operating point is unstable.

 $\bullet \qquad \mbox{ChangesinV}_{be} \mbox{ will change}_B \mbox{ and thus cause} R_E to \mbox{ change}. This inturn will alter the gain of the stage. \label{eq:change}$

• Whenthetransistoris replaced with another one, considerable change in the value of β can be expected. Due to this change the operating point will shift.

2) EMITTER-FEEDBACKBIAS:

The emitter feedback bias circuit is shown in the fig 2.15. The fixed bias circuit is modified by attaching an external resistor to the emitter. This resistor introduces negative feedback that stabilizes the Q-point. From Kirchhoff's voltage law, the voltage across the base resistor is

V_{Rb}=V_{CC}-I_eR_e-V_{be}.



Fig2.15SelfBiasing Circuit

FromOhm'slaw, the base current is

 $I_b = V_{Rb}/R_b$.

The way feedback controls the bias point is as follows. If V_{be} is held constant and temperature increases, emitter current increases. However, a larger I_e increases the emitter voltage $V_e = I_e R_e$, which in turn reduces the voltage V_{Rb} across the baseresistor. A lower base-resistor voltaged rop reduces the base current, which results in less collector current because $I_c = \beta I_B$. Collector current and emitter current are related by $I_c = \alpha I_e$ with $\alpha \approx 1$, so increase in emitter current with temperature is opposed, and operating point is kept stable.

Similarly, if the transistoris replaced by another, there may be change in β -value, for example). By similar process as above, the change is negated and operating point kept stable.

Forthegivencircuit,

 $I_B = (V_{CC} - V_{be}) / (R_B + (\beta + 1)R_E).$

Merits:

 $The circuit has the tendency to stabilize operating point against changes in temperature and \beta-value. \\$

Demerits:

• Inthiscircuit,tokeeplcindependentofβthefollowingconditionmustbemet:

$$I_{C} = \beta I_{B} = \frac{\beta (V_{CC} - V_{be})}{R_{B} + (\beta + 1)R_{E}} \approx \frac{(V_{CC} - V_{be})}{R_{E}}$$

which is approximately the case if $(\beta + 1)R_E >> R_B$.

 $\bullet \qquad As\beta-value is fixed for a given transistor, this relation can be satisfied either by keeping R_{\rm E} very large, or making R_{\rm B} very low.$

 $\bullet \qquad \mbox{If} R_{E} \mbox{ isoflarge} value, \mbox{high} V_{CC} \mbox{ isnecessary}. This increases cost as well as precautions necessary while \mbox{handling}.$

• If R_B is low, as eparatelow voltage supply should be used in the base circuit. Using two supplies of different voltages is impractical.

 $\bullet \qquad \mbox{Inadditiontotheabove}, R_E \mbox{causes acfeed backwhich reduces the voltage gain of the amplifier}.$

3) COLLECTORTOBASEBIASORCOLLECTORFEED-BACKBIAS:



Fig2.16CollectortoBaseBiasingCircuit

This configuration shown in fig2.16 employs negative feedback to prevent thermal runaway and stabilize the operating point. In this form of biasing, the base resistor $R_{\rm B}$ is connected to the collector instead of connecting it to the DC source $V_{\rm cc}$. So any thermal runaway will induce a voltage drop across the $R_{\rm C}$ resistor that will throttle the transistor's base current.

From Kirchhoff's voltage law, the voltage $V_{
m R_b}$ across the base resistor $R_{
m b}$ is

 $V_{\rm R_b} = V_{\rm cc} - \underbrace{\overbrace{(I_{\rm c} + I_{\rm b})R_{\rm c}}^{\rm Voltage \ drop \ across \ R_{\rm c}}_{\rm V_{\rm be}} - \underbrace{V_{\rm obt}}_{V_{\rm be}}^{\rm Voltage \ at \ base}$

By the Ebers–Mollmodel, $I_c = \beta I_b$, and so

$$V_{\rm R_b} = V_{\rm cc} - (\overbrace{\beta I_{\rm b}}^{I_{\rm c}} + I_{\rm b})R_{\rm c} - V_{\rm be} = V_{\rm cc} - I_{\rm b}(\beta + 1)R_{\rm c} - V_{\rm be}.$$

FromOhm'slaw,thebasecurrent $I_{
m b}=V_{
m R_b}/R_{
m b}$,andso

$$\overbrace{I_{\rm b}R_{\rm b}}^{V_{\rm R_{\rm b}}} = V_{\rm cc} - I_{\rm b}(\beta+1)R_{\rm c} - V_{\rm be}$$

Hence, the base current *I*_b is

$$I_{\rm b} = \frac{V_{\rm cc} - V_{\rm be}}{R_{\rm b} + (\beta + 1)R_{\rm c}}$$

If V_{be} is held constant and temperature increases, then the collector current I_c increases. However, a larger I_c causes the voltaged rop across resistor R_c to increase, which in turn reduces the voltage V_{Rb} across the base resistor R_b . A lower base-resistor voltage drop reduces the base current I_b , which results in less collector current I_c . Because an increase in collector current with temperature is opposed, the operating point is kept stable.

Merits:

• Circuit stabilizes the operating point against variations in temperature and β (i.e. replacement of transistor)

Demerits:

• Inthiscircuit,tokeep*I*cindependentofβ,thefollowingconditionmustbemet:

$$I_{\rm c} = \beta I_{\rm b} = \frac{\beta (V_{\rm cc} - V_{\rm be})}{R_{\rm b} + R_{\rm c} + \beta R_{\rm c}} \approx \frac{(V_{\rm cc} - V_{\rm be})}{R_{\rm c}}$$

whichisthecasewhen

 $\beta R_{\rm c} \gg R_{\rm b}$.

• As β -value is fixed (and generally unknown) for a given transistor, this relation can besatisfied either by keeping R_c fairly large or making R_b very low.

• If R_c is large, a high V_{cc} is necessary, which increases cost as well as precautions necessary while handling.

• If *R*_b is low, the reverse bias of the collector–base region is small, which limits the range of collector voltage swing that leaves the transistor in active mode.

• The resistor R_b causes an AC feedback, reducing the <u>voltage gain</u> of the amplifier. This undesirable effect is a trade-off for greater <u>Q-point</u> stability.

Usage: The feedback also decreases the inputimpedance of the amplifier as seen from the base, which can be advantageous. Due to the gain reduction from feedback, this biasing form is used only when the trade-off for stability iswarranted.

4) COLLECTOR-EMITTERFEEDBACKBIAS:



Fig2.17Collector-EmitterBiasingCircuit

The above fig 2.17shows the collector –emitter feedback bias circuit that can be obtained by applying both the collector feedback and emitter feedback. Here the collector feedback is provided by connecting a resistance RB from the collector to the base and emitter feedback is provided by connecting an emitter Re from emitter to ground. Both feed backs areused tocontrol collectorcurrent and base current IB in the opposite direction to increase the stability as compared to the previous biasingcircuits.

5) VOLTAGEDIVIDERBIASORSELFBIASOREMITTERBIAS

The voltage divider as shown in the fig 2.18 is formed using external resistors R_1 and R_2 . The voltage across R_2 forward biases the emitter junction. By proper selection of resistors R_1 and R_2 , the operating pointofthetransistorcanbe made independentof β .Inthiscircuit,thevoltagedividerholds the base voltage fixed independent of base current provided the divider current is large compared to the base current. However, even with a fixed base voltage, collector current varies with temperature (for example) so an emitter resistor is added to stabilize the Q-point, similar to the above circuits with emitter resistor.



Fig2.18VoltageDividerBiasingCircuit

Inthiscircuitthebasevoltageisgivenby:

$$V_{B} =_{\text{voltageacross}} R_{2}^{=} V_{cc} \frac{R_{2}}{(R_{1} + R_{2})} - I_{B} \frac{R_{1}R_{2}}{(R_{1} + R_{2})}$$
$$\approx V_{cc} \frac{R_{2}}{(R_{1} + R_{2})}_{\text{provided}} I_{B} << I_{2} = V_{B}/R_{2}.$$

$$_{\mathsf{Also}}V_B = V_{be} + I_E R_E$$

Forthegivencircuit,

$$I_B = \frac{\frac{V_{CC}}{1+R_1/R_2} - V_{be}}{(\beta+1)R_E + R_1 \parallel R_2}.$$

Let the current in resistor R1 is I1 and this is divided into two parts – current through base and resistor R2. Since the base current is very small so for all practical purpose it is assumed that I1 also flows through R2, so we have

$$I_1 = \frac{V_{CC}}{R_1 + R_2}$$
$$V_2 = \frac{V_{CC}}{R_1 + R_2} \cdot R_2$$

ApplyingKVLinthecircuit, we have

$$V_2 = V_{BE} + V_E$$
$$V_2 = V_{BE} + I_E R_E$$

$$I_E = \frac{V_2 - V_{BE}}{R_E}$$

$$I_C = \frac{V_2 - V_{BE}}{R_E} \quad \because I_C \cong I_E$$

$$I_C = \frac{\frac{V_2 - V_{BE}}{R_E} \cdot R_2 - V_{BE}}{R_E}$$

It is apparent from above expression that the collector current is independent of ? thus the stability is excellent. In all practical cases the value of VBE is quite small in comparison to the V2, so it can be ignoredinthe above expression so the collector current is almost independent of the transistor parameters thus this arrangement provides excellent stability.

AgainapplyingKVLincollectorcircuit, we have

$$V_{CC} = I_C R_C + V_{CE} + I_E R_E$$

$$\therefore I_C \cong I_E$$

$$\therefore V_{CC} = I_C R_C + V_{CE} + I_C R_E$$

$$V_{CE} = V_{CC} - I_C (R_C + R_E)$$

The resistor RE provides stability to the circuit. If the current through the collector rises, the voltage across the resistor RE also rises. This will cause VCE to increase as the voltage V2is independent of collector current. This decreases the base current, thus collector currentincreases to its formervalue.

Stabilityfactorforsuchcircuitarrangementisgivenby

$$S = \frac{(1+\beta)(R_{eq} + R_E)}{R_{eq} + R_E(1+\beta)}$$
$$R_{eq} = R_1 ||R_2$$
$$S = \frac{(1+\beta)\left(1 + \frac{R_{eq}}{R_E}\right)}{\frac{R_{eq}}{R_E} + 1 + \beta}$$

IfReq/REisverysmallcomparedto1, it can be ignored in the above expression thus we have

$$S = \frac{1+\beta}{1+\beta} = 1$$

Which is excellent since it is the smallest possible value for the stability. In actual practice the value ofstability factor is around 8-10, since Req/REcannot be ignored as compared to 1.

Merits:

- Unlikeabovecircuits, only oned csupply is necessary.
- Operatingpointisalmostindependentofβvariation.
- Operatingpointstabilizedagainstshiftintemperature.

Demerits:

• Inthiscircuit,tokeepl_cindependentofβthefollowingconditionmustbemet:

$$I_C = \beta I_B = \beta \frac{\frac{V_{CC}}{1+R_1/R_2} - V_{be}}{(\beta+1)R_E + R_1 \parallel R_2} \approx \frac{\frac{V_{CC}}{1+R_1/R_2} - V_{be}}{R_E},$$

which is approximately the case if $(eta+1)R_E>>R_1\parallel R_2$

 $where R_1 \mid \mid R_2 denotes the equivalent resistance of R_1 and R_2 connected in parallel.$

• As β -value is fixed for a given transistor, this relation can be satisfied either by keeping R_E fairly large, or making R₁||R₂verylow.

• If R_E is of large value, high V_{CC} is necessary. This increases cost as well as precautions necessary whilehandling.

• If $R_1 \mid \mid R_2$ is low, either R_1 is low, or R_2 is low, or both are low. A low R_1 raises V_B closer to V_C , reducing the available swing in collector voltage, and limiting how large R_C can be made without driving the transistor out of active mode. A low R_2 lowers V_{be} , reducing the allowed collector current. Lowering both resistor values draws more current from the power supply and lowers the input resistance of the amplifier as seen from thebase.

• AC as well as DC feedback is caused by R_E , which reduces the AC voltage gain of the amplifier. A method to avoid AC feedback while retaining DC feedback is discussed below.

 ${\it Usage:} The circuit's stability and merits as above make it widely used for linear circuits.$

BIASCOMPENSATIONUSINGDIODEANDTRANSISTOR

The various biasing circuits considered use some type of negative feedback to stabilize the operation point. Also, diodes, thermistors and sensistors can be used to compensate for variations in current.

DIODECOMPENSATION:



Fig2.19DiodeCompensationCircuit

The following fig 2.19 shows a transistor amplifier with a diode D connected across the baseemitter junction for compensation of change in collector saturation current I_{CO} . The diode is of the same material as the transistor and it is reverse biased by e the emitter-base junction voltage V_{BE} , allowing the diode reverse saturation current I_{O} to flow through diode D. The base current $I_{B}=I-I_{O}$.

As long as temperature is constant, diode D operates as a resistor. As the temperature increases, I_{CO} of the transistor increases. Hence, to compensate for this, the base current I_B should be decreased.

The increase in temperature will also cause the leakage current I_0 through D to increase and thereby decrease the base current I_B . This is the requiredaction to keep Ic constant.

This type of biascompensation does not need a change in Ic to effect the change in I_{c} , as both I_{co} can track almost equally according to the change intemperature.

THERMISTORCOMPENSATION:

The following fig2.20 athermistor R_T , having a negative temperature coefficient is connected in parallel with R_2 . The resistance of thermistor decreases exponentially with increase of temperature. An increase of temperature will decrease the base voltage V_{BE} , reducing I_B and I_C .



Fig2.20ThermistorCompensation

SENSISTORCOMPENSATION:

In the following fig2.21 shown a sensistor Rs having a positive temperature coefficient is connected across R₁or R_E. Rs increases with temperature. As the temperatureincreases, the equivalent resistance of the parallel combination of R1 and Rs also increases and hence V_{BE}decreases, reducing I_B and Ic. This reduced Ic compensates for increased Ic caused by the increase in V_{BE}, I_{CO} and β due totemperature.



Fig2.21SensistorCompensation

BJT Hybrid Model and Transistor Amplifier

BJTHybridModelandTransistorAmplifier's-parameterrepresentationofatransistor, Conversion of h-parameters, Analysis of single stage transistor amplifier using H-parameters:voltagegain,currentgain,InputimpedanceandOutputimpedance. Comparison of transistor configurations in terms of Ai, Ri, Av, and Ro,

BJTHYBRIDMODEL

SmallsignallowfrequencytransistorModels:

Allthe transistor amplifiers are two port networks having twovoltages and two currents. The positive directions of voltages and currents are shown in **fig. 1**.



Fig.3.1:TransistorasatwoportNetwork

A two-port network is represented by fourexternalvariables:voltage V_1 and current I_1 at the input port, and voltage V_2 and current I_2 at the output port, so that the two-port network can be treated as a black box modeled by the relationships between the four variables, V_1 , V_2 , I_1 , I_2 . Out of four variables two can be selected as are independent variables and two are dependent variables. The dependent variables can be expressed interns of independent variables. This leads to various two port parameters out of which the following three are important:

- 1. Impedanceparameters(z-parameters)
- 2. Admittanceparameters(y-parameters)
- 3. Hybridparameters(h-parameters)

z-parameters

Atwo-port networkcanbedescribedbyz-parametersas

 $\begin{aligned} V_1 &= Z_{11}I_1 + Z_{12}I_2 \\ V_2 &= Z_{21}I_1 + Z_{22}I_2 \end{aligned}$

Inmatrixform, the above equation can be rewritten as

$\begin{bmatrix} V_1 \end{bmatrix}_{-}$	z_{11}	z_{12}	$[I_1]$
V_2	z_{21}	z_{22}	I_2

Where

$$z_{11} = \left. \frac{V_1}{I_1} \right|_{I_2 = 0}$$

Inputimpedancewithoutputportopencircuited

$$z_{12} = \left. \frac{V_1}{I_2} \right|_{I_1=0}$$

Reverse transfer impedance with input port open circuited

$$z_{21} = \left. \frac{V_2}{I_1} \right|_{I_2=0}$$

 $\label{eq:Forward} Forward transfer impedance without put port open circuited$

$$z_{22} = \left. \frac{V_2}{I_2} \right|_{I_1=0}$$

Outputimpedancewithinputportopencircuited

Y-parameters

Atwo-portnetworkcanbedescribedbyY-parametersas

$$\begin{split} I_1 &= Y_{11}V_1 + Y_{12}V_2 \\ I_2 &= Y_{21}V_1 + Y_{22}V_2 \end{split}$$

Inmatrixform, the above equation can be rewritten as

$$\begin{bmatrix} I_1 \\ I_2 \end{bmatrix} = \begin{bmatrix} y_{11} & y_{12} \\ y_{21} & y_{22} \end{bmatrix} \begin{bmatrix} V_1 \\ V_2 \end{bmatrix}$$
$$y_{11} = \left. \frac{I_1}{V_1} \right|_{V_2 = 0}$$

Inputadmittancewithoutputportshortcircuited

$$y_{12} = \left. \frac{I_1}{V_2} \right|_{V_1=0}$$

Reverse transfer admittance with input portshort circuited

$$y_{21} = \left. \frac{I_2}{V_1} \right|_{V_2 = 0}$$

 $\label{eq:Forward} Forward transfer admittance without put portshort circuited$

$$y_{22} = \left. \frac{I_2}{V_2} \right|_{V_1 = 0}$$

Outputadmittancewithinputportshortcircuited

Hybridparameters(h-parameters)

If the input current I1 and output voltage V2 are taken as independent variables, the dependent variables V1 and I2 can be written as

 $\begin{bmatrix} V_1 \\ I_2 \end{bmatrix} = \begin{bmatrix} h_{11} & h_{12} \\ h_{21} & h_{22} \end{bmatrix} \begin{bmatrix} I_1 \\ V_2 \end{bmatrix}$

 $Where h_{11}, h_{12}, h_{21}, h_{22} are called a shybrid parameters.$

$$h_{11} = \left. \frac{V_1}{I_1} \right|_{V_2 = 0}$$

Inputimpedencewitho/pportshortcircuited

$$h_{12} = \left. \frac{V_1}{V_2} \right|_{I_1=0}$$

Reversevoltagetransferratiowithi/pport opencircuited

$$h_{21} = \left. \frac{I_2}{I_1} \right|_{V_2=0}$$

Forwardvoltagetransferratiowitho/pportshortcircuited

$$h_{22} = \left. \frac{I_2}{V_2} \right|_{I_1=0}$$

outputimpedencewithi/pportopencircuited

THEHYBRID MODELFORTWOPORTNETWORK:

Basedonthe definition of hybrid parameters the mathematical model for two pertnetworks known as hparameter model can be developed. The hybrid equations can be written as: $V_1 = h_i I_1 + h_r V_2$

 $I_2 = h_f I_1 + h_o V_2$

(Thefollowingconvenientalternativesubscriptnotationis recommended by the IEEE Standards: *i*=11=input *o*=22=output

f=21=forwardtransferr=12=reversetransfer)

We may now use the four h parameters to construct a mathematicalmodel of the device of Fig.(1). The hybrid circuit for any device indicated in Fig.(2). We can verify that the model of Fig.(2) satisfies above equations by writing Kirchhoff'svoltage and current laws for input and output ports.



If these parameters are specified for a particular configuration, then suffixes e, bor care also included, e.g. h_{fe}, h_{ib} are hparameters of common emitter and common collector amplifiers

 $Using two equations the generalized model of the amplifier can be drawn as shown in \underline{fig. 3.2}.$



Fig.3.2:-h-parameterequivalentofTransistor

TRANSISTORHYBRIDMODEL:

Thehybridmodelforatransistoramplifiercanbederivedas follow:

 $Let us consider CE configuration as showin \underline{fig. 3.3}. The variables, i_{B}, i_{C}, v_{C}, and v_{B} represent to tal instantaneous currents and voltages i_{B} and v_{C} can be taken as independent variables and v_{B}, l_{C} as dependent variables.$



Fig.3.3CETransistorAmplifier V_B

 $I_C = f2(i_B, v_C).$

Using Taylor's series expression, and neglecting higher order terms we obtain.

$$\Delta v_{B} = \frac{\partial f_{1}}{\partial i_{B}} \bigg|_{V_{C}} \Delta i_{B} + \frac{\partial f_{1}}{\partial v_{C}} \bigg|_{i_{B}} \Delta v_{C}$$
$$\Delta i_{C} = \frac{\partial f_{2}}{\partial i_{B}} \bigg|_{V_{C}} \Delta i_{B} + \frac{\partial f_{2}}{\partial v_{C}} \bigg|_{i_{B}} \Delta v_{C}$$

Thepartial derivatives aretakenkeepingthe collectorvoltageor basecurrent constant. The Δv_{B} , Δv_{C} , Δi_{B} , Δi_{C} represent the small signal (incremental) base and collector current and voltage and can be represented as v_{B}, i_{C}, i_{B}, v_{C}

where

$$\begin{aligned} h_{ie} &= \frac{\partial f_1}{\partial i_B} \bigg|_{v_c} &= \left. \frac{\partial v_B}{\partial i_B} \right|_{v_c}; \qquad h_{re} &= \left. \frac{\partial f_1}{\partial v_C} \right|_{i_B} &= \left. \frac{\partial v_B}{\partial v_C} \right|_{i_B} \\ h_{fe} &= \left. \frac{\partial f_2}{\partial i_B} \right|_{v_c} &= \left. \frac{\partial i_C}{\partial i_B} \right|_{v_c}; \qquad h_{oe} &= \left. \frac{\partial f_2}{\partial v_C} \right|_{i_B} &= \left. \frac{\partial v_B}{\partial v_C} \right|_{i_B} \end{aligned}$$



Fig.3.4:h-parametermodelofCEConfiguration

To determine the four h-parameters of transistor amplifier, input and output characteristic are used. Input characteristic depicts the relationship between input voltage and input current with output voltage as parameter. The output characteristic depicts the relationship between output voltage and output current with input current as parameter. <u>Fig. 5</u>, shows the output characteristicsofCE amplifier.



Fig.3.5TransistorCEConfigurationoutputcharacteristics

The current increments are taken around the quiescent point Q which corresponds to i_B = I_B and to the collector voltage V_{CE} = V_C

$$h_{oe} = \frac{\partial i_C}{\partial V_C} \Big|_{i_B}$$

Thevalue of h_{oe} at the quiescent operating point is given by the slope of the output characteristicat the operating point (i.e. slope of tangent AB).

$$\mathsf{h}_{\mathsf{ie}} = \left. \frac{\partial \mathsf{V}_{\mathsf{B}}}{\partial \mathsf{i}_{\mathsf{B}}} \right| \approx \left. \left. \frac{\Delta \mathsf{V}_{\mathsf{B}}}{\Delta \mathsf{i}_{\mathsf{B}}} \right|_{\mathsf{V}_{\mathsf{C}}}$$

 $h_{ie} is the slope of the appropriate input on \underline{fig. 3.6}, at the operating point (slope of tangent EF at Q).$

$$h_{re} = \frac{\partial V_B}{\partial V_C} = \frac{\Delta V_B}{\Delta V_C} \Big|_B = \frac{V_{B2} - V_{B1}}{V_{C2} - V_{C1}}$$

$$V_{B1}$$

$$V_{C1}$$

$$V_{C1}$$

$$V_{C2}$$

Fig.3.6Calculationofh-parameters from output characteristics

Averticalline on the input characteristic represents constant base current. The parameter hrecan be obtained from the ratio $(V_{B2} - V_{B1})$ and $(V_{C2} - V_{C1})$ for at Q.

TypicalCEh-parametersoftransistor2N1573aregivenbelow:

h_{ie}= 1000ohm. h_{re}=2.5*10-4 h_{fe}=50 h_{oe}=252A/V

ANALYSISOFATRANSISTORAMPLIFIERUSINGH-PARAMETERS:

Toforma transistoramplifierit isonlynecessarytoconnectanexternalloadandsignalsourceas indicated in <u>fig. 3.7</u> and to bias the transistor properly.



Fig.3.7Transistor two port Network

Consider the two-port network of CEamplifier. R_s is the source resistance and Z_L is the loadimpedence hparameters are assumed tobe constant over the operating range. The ac equivalent circuit is shown in fig. 2. (Phasor notations are used assuming sinusoidal voltage input). The quantities of interest are the current gain, input impedence, voltage gain, and output impedence.



Fig3.8:hparameterequivalent of TransistorinCE configuration **Current gain:**

Forthetransistoramplifierstage, Aisdefined astheratioofoutputtoinputcurrents.

$$A_{I} = \frac{I_{L}}{I_{1}} = \frac{-I_{2}}{I_{1}}$$

Inputimpedence:

Theimpedence lookingintotheamplifierinputterminals(1,1')istheinputimpedanceZ_i

$$\begin{split} Z_i &= \frac{v_b}{l_b} \\ V_b &= h_{ie} l_b + h_{re} V_c \\ \frac{V_b}{l_b} &= h_{ie} + h_{re} \frac{V_c}{l_b} \\ &= h_{ie} - \frac{h_{re} l_c Z_L}{l_b} \\ \therefore Z_i &= h_{ie} + h_{re} A_I Z_L \\ &= h_{ie} - \frac{h_{re} h_{fe} Z_L}{1 + h_{oe} Z_L} \\ \therefore Z_i &= h_{ie} - \frac{h_{re} h_{fe}}{Y_L + h_{oe}} \quad (\text{since } Y_L = \frac{1}{Z_L}) \end{split}$$

Voltagegain:

The ratio of output voltage to input voltage gives the gain of the transistors.

$$A_{v} = \frac{V_{C}}{V_{b}} = -\frac{I_{C}Z_{L}}{V_{b}}$$
$$\therefore A_{v} = \frac{I_{B}A_{i}Z_{L}}{V_{b}} = \frac{A_{i}Z_{L}}{Z_{i}}$$

Output Admittance:

$$\begin{aligned} Y_{0} &= \frac{I_{c}}{V_{c}} \bigg|_{V_{s}} = 0 \\ I_{c} &= h_{fe}I_{b} + h_{oe} V_{c} \\ \frac{I_{c}}{V_{c}} &= h_{fe} \frac{I_{b}}{V_{c}} + h_{oe} \\ when V_{s} = 0, \qquad R_{s}.I_{b} + h_{ie}.I_{b} + h_{re}V_{c} = 0. \\ \frac{I_{b}}{V_{c}} &= -\frac{h_{re}}{R_{s} + h_{ie}} \\ \therefore Y_{0} &= h_{oe} - \frac{h_{re} - h_{fe}}{R_{s} + h_{ie}} \end{aligned}$$

Voltage amplification taking into account source impedance (R_S) is given by

$$A_{VS} = \frac{V_c}{V_s} = \frac{V_c}{V_b} * \frac{V_b}{V_S} \qquad \left(V_b = \frac{V_s}{R_s + Z_i} * Z_i\right)$$
$$= A_{V} \cdot \frac{Z_i}{Z_i + R_s}$$
$$= \frac{A_i Z_L}{Z_i + R_s}$$

Itisdefinedas

Avisthevoltagegainforanidealvoltagesource(Rv=0).

Considerinputsourcetobeacurrentsourcelsinparallelwitha resistanceRsasshowninfig.3.



In this case, overall current gain A_{IS} is defined as

$$\begin{aligned} A_{I_{s}} &= \frac{I_{L}}{I_{s}} \\ &= -\frac{I_{c}}{I_{s}} \\ &= -\frac{I_{c}}{I_{b}} * \frac{I_{b}}{I_{s}} \qquad \left(I_{b} = \frac{I_{s} * R_{s}}{R_{s} + Z_{i}}\right) \\ &= A_{I} * \frac{R_{s}}{R_{s} + Z_{i}} \\ & \text{If } R_{s} \to \infty, \qquad A_{T_{s}} \to A_{T} \end{aligned}$$

h-parameters

Toanalyzemultistageamplifiertheh-parameters of the transistor used are obtained from manufacture datasheet. The manufacture datasheet usually providesh-parameterin CE configuration. These parameters may be converted into CC and CB values. For example <u>fig. 4</u> hrc in terms of CE parameter canbeobtained as follows.



Fig.3.9CEh-parametermodel

ForCEtransistorconfiguaration Vbe

= hie lb + hre Vce

Ic=hfelb+hoe Vce

The circuit can be redrawn like CC transistor configuration as shown in fig.5. Vbc =

hie Ib + hrc Vec

Ic=hfeIb+hoeVec





Typicalh-parametervaluesforatransistor

Parameter	CE	CC	СВ
h _i	1100Ω	1100 Ω	22 Ω
h _r	2.5×10 ⁻⁴	1	3×10 ⁻⁴
h _f	50	-51	-0.98
ho	25µA/V	25µA/V	0.49µA/V

AnalysisofaTransistoramplifiercircuitusingh-parameters

A transistoramplifiercanbe constructed by connecting anexternal load and signal source and biasing the transistor properly.



Fig.3.11BasicAmplifierCircuit

The two port network of Fig. 3.11 represents a transistor in any one of its configuration. It is assumed thath-parameters remain constant over the operating range. The input is sinusoidal and I_1, V_{-1}, I_2 and V_2 are phase quantities



Fig.3.12TransistorreplacedbyitsHybridModel

CurrentGainorCurrentAmplification(A_i)

For transistor amplifier the current gain A_i is defined as the ratio of output current to input current, i.e,

$$A_i = I_L / I_1 = -I_2 / I_1$$

FromthecircuitofFig

 $I_2 = h_f I_1 +$

 $h_0V_2Substitutin$

 $g V_2 = I_L Z_L = -I_2 Z_L$

 $I_2=h_fI_1-I_2Z_Lh_o$

$$I_2 + I_2 Z_L h_o = h_f$$

 $I_1I_2(1+Z_Lh_o)=h_fI_1$

 $A_i = -I_2/I_1 = -h_f/(1 + Z_L h_o)$ Therefore,

 $A_i = -h_f / (1 + Z_L h_o)$

InputImpedence(Z_i)

In the circuitof Fig ,R_sisthesignalsourceresistance.Theimpedenceseenwhenlookingintothe amplifier terminals (1,1[']) is the amplifier input impedenceZ_i,

 $Z_i=V_1/I_1$

From the input circuit of Fig $V_1 = h_i I_1 + h_r V_2 Z_i =$

 $(h_i I_1 + h_r V_2) / I_1$

=h_i+h_rV₂/I₁Substituting

 $V_2 = -I_2 Z_L = A_1 I_1 Z_L$

 $Z_i = h_i + h_r A_1 I_1 Z_L / I_1$

 $= h_i + h_r$

 $A_1Z_LSubstitutingf \\$

 $\text{or}A_i$

 $Z_i=h_i-h_fh_rZ_L/(1+h_oZ_L)$

 $=h_i-h_fh_rZ_L/Z_L(1/Z_L+h_o)$

 $Taking the Load admittance as Y_L = 1/Z_L Z_i =$

 $h_i - h_f h_r / (Y_L + h_o)$

VoltageGainorVoltageGainAmplificationFactor(A_v)

The ratio of output voltage V₂to input voltage V₁give the voltage gain of the transistor i.e,

$$A_v = V_2 / V_1$$

Substituting

$$V_2 = -I_2 Z_L = A_1 I_1 Z_L$$

$$A_v = A_1 I_1 Z_L / V_1 = A_i Z_L / Z_i$$

OutputAdmittance(Y_o)

 Y_0 is obtained by setting V_s to zero, Z_L to infinity and by driving the output terminals from a generator V_2 . If the current V_2 is I_2 then $Y_0 = I_2/V_2$ with $V_s = 0$ and $R_L = \infty$.

Fromthecircuitoffig

 $I_2 = h_f I_1 + h_o V_2 Dividing$

by V_{2,}

 $I_2/V_2=h_fI_1/V_2+h_o$

WithV2=0,byKVL ininputcircuit,

 $R_{S}I_{1}+h_{i}I_{1}+h_{r}V_{2}=0$ (R_{S}

 $+ h_i$) I₁ + h_rV₂= 0

Hence, $I_2/V_2 = -h_r/(R_s + h_i)$

$$=h_f(-h_r/(R_s+h_i)+h_oY_o=h_o-$$

 $h_f h_r / (R_s + h_i)$

Theoutputadmittance isafunctionofsourceresistance. If the source impedence is resistive then Yois real.

$Voltage Amplification Factor (A_{vs}) taking into account the resistance (R_s) of the source$



Fig.3.13 Thevenin's EquivalentInput

Circuit This overall voltage gain Avsis given by

 $A_{vs}=V_2/V_s=V_2V_1/V_1V_s=A_vV_1/V_s$

From the equivalent input circuit using The venin's equivalent for the sources hown in Fig. 5.6 V1 =

 $V_{s}Z_{i}/(Z_{i+}R_{s})$ $V_{1}/V_{s}=Z_{i}/(Z_{i}+R_{s})$

Then, $A_{vs}=A_vZ_i/(Z_i+R_s)$

Substituting $A_v = A_i Z_L / Z_i$

 $A_{vs}=A_iZ_L/(Z_i+R_S)$

 $A_{vs}=A_iZ_LR_S/(Z_i+R_S)R_S$

 $A_{vs} = A_{is}Z_L/R_S$

CurrentAmplification(A_{is})takingintoaccountthesourceResistance(R_s)



Fig.3.14Norton'sEquivalentInputCircuit

Themodified input circuit using Norton's equivalent circuit for the calculation of A_{is} is shown in Fig. 1.7 Overall

Current Gain, A_{is} = - I_2/I_s = - I_2I_1/I_1I_s = A_iI_1/I_s

FromFig.1.7

 $I_1 = I_S R_S / (R_S + Z_i) I_1$ / $I_S = R_S / (R_S + Z_i)$ $A_{is} = A_i R_S / (R_S + Z_i)$

andhence,

OperatingPowerGain(A_P)

The operating power gain A_Pof the transistor is defined as

$$A_P = P_2 / P_1 = -V_2 I_2 / V_1 I_1 = A_v A_i = A_i A_i Z_L / Z_i$$

 $A_P = A_i^2 (Z_L / Z_i)$

SmallSignalanalysisofatransistor amplifier

$A_i = -h_f / (1 + Z_L h_o)$	$A_v = A_i Z_L / Z_i$
$Z_i = h_i + h_r A_1 Z_L = h_i - h_f h_r / (Y_L + h_o)$	$A_{vs}=A_vZ_i/(Z_i+R_s)=A_iZ_L/(Z_i+R_s)$ $=A_{is}Z_L/R_s$
$Y_o=h_o-h_fh_r/(R_s+h_i)=1/Z_o$	$A_{is}=A_iR_s/(R_s+Z_i)=A_{vs}=A_{is}R_s/Z_L$

UNIT -II BJT AMPLIFIERS FREQUIENCY RESPONCE(HYBRIDE PI MODEL)

UNIT I

Small Signal High Frequency Transistor Amplifier models

BJT: Transistor at high frequencies, Hybrid- π common emitter transistor model, Hybrid π conductances, Hybrid π capacitances, validity of hybrid π model, determination of high-frequency parameters in terms of low-frequency parameters, CE short circuit current gain, current gain with resistive load, cut-off frequencies, frequency response and gain bandwidth product. **FET:** Analysis of common Source and common drain Amplifier circuits at high frequencies.

Introduction:

Electronic circuit analysis subject teaches about the basic knowledge required to design an amplifier circuit, oscillators etc .It provides a clear and easily understandable discussion of designing of different types of amplifier circuits and their analysis using hybrid model, to find out their parameters. Fundamental concepts are illustrated by using small examples which are easy to understand. It also covers the concepts of MOS amplifiers, oscillators and large signal amplifiers.

Two port devices & Network Parameters:

A transistor can be treated as a two-part network. The terminal behavior of any two-part network can be specified by the terminal voltages V1& V2at parts 1 & 2 respectively and current i1and i2, entering parts 1 & 2, respectively, as shown in figure.



Of these four variables V1, V2, i1and i2, two can be selected as independent variables and the remaining two can be expressed in terms of these independent variables. This leads to various two part parameters out of which the following three are more important.

- 1. Z Parameters (or) Impedance parameters
- 2. Y Parameters (or) Admittance parameters
- 3. H Parameters (or) Hybrid parameters

Hybrid parameters (or) h -parameters:

The equivalent circuit of a transistor can be dram using simple approximation by retaining its essential features. These equivalent circuits will aid in analyzing transistor circuits easily and rapidly.

If the input current i_1 and output Voltage V_2 are takes as independent variables, the input voltage V_1 and output current i_2 can be written as

 $V_1 = h_{11} i_1 + h_{12} V_2$ $i_2 = h_{21} i_1 + h_{22} V_2$

The four hybrid parameters h11, h12, h21and h22 are defined as follows:

h11= [V1/i1] with V2= 0 Input Impedance with output part short circuited. h22= [i2/V2] with i1= 0 Output admittance with input part open circuited. h12= [V1/V2] with i1= 0 reverse voltage transfer ratio with input part open circuited. h21= [i2/i1] with V2= 0 Forward current gain with output part short circuited

The dimensions of h-parameters are as follows:

h11**-**Ω

h22-mhos

h12, h21 -dimension less.

As the dimensions are not alike, (i.e.) they are hybrid in nature, and these parameters are called as hybrid parameters.

h11 = input; h 22 = output; h21= forward transfer; h22 = Reverse transfer.
Notations used in transistor circuits:

 h_{ie} = h11e= Short circuit input impedance h_{oe} = h22e= Open circuit output admittance h_{re} = h12e= Open circuit reverse voltage transfer ratio h_{fe} = h21e= Short circuit forward current Gain.

The Hybrid Model for Two-port Network:

```
V1=h11 i1+h12V2 
I2=h21i1+h22V2 
V1=h_1i1+h_rV2 
I2=h_fi1+h_0V2
```



Common Emitter Amplifier

Common Emitter Circuit is as shown in the Fig. The DC supply, biasing resistors and coupling capacitors are not shown since we are performing an AC analysis.



 $E_{s}\xspace$ is the input signal source and $R_{s}\xspace$ is the resistance. The h-parameter equivalent for the above circuit is as shown in Fig.



The typical values of the h-parameter for a transistor in Common Emitter configuration are,

$$h_{ie} = \frac{V_{be}}{I_b}$$
$$h_{ie} = \frac{0.2V}{50 \times 10^{-6}} = 4K\Omega$$

$$h_{fe} = I_c / I_b \simeq 100 .$$
$$h_{fe} >> 1 \simeq \beta$$

$$\begin{split} \mathbf{h}_{\mathrm{re}} &= \frac{\mathbf{V}_{\mathrm{be}}}{\mathbf{V}_{\mathrm{ce}}} \\ \mathbf{h}_{\mathrm{re}} &= 0.2 \times 10^{-3}, \\ \mathbf{h}_{\mathrm{oe}} &= \frac{\mathbf{I}_{\mathrm{c}}}{\mathbf{V}_{\mathrm{ce}}}. \end{split}$$

$$h_{oe} = 8 \mu \mho$$

$$R_{i} = h_{ie} - \frac{h_{fe}h_{re}}{h_{oe} + \frac{1}{R_{L}}}$$

$$R_{i} = h_{ie} - \frac{h_{fe}h_{re}}{h_{oe} + \frac{1}{R_{L}}}$$

$$R_{o} = \frac{1}{h_{oe} - \left(\frac{h_{re}h_{fe}}{h_{ie} + R_{s}}\right)}$$

$$A_{i} = \frac{-h_{fe}}{1+h_{oe}R_{L}}$$

$$A_{V} = \frac{-h_{fe}R_{L}}{h_{ie} + R_{L}(h_{ie}h_{oe} - h_{fe}h_{re})}$$

Common Base Amplifier

Common Base Circuit is as shown in the Fig. The DC supply, biasing resistors and coupling capacitors are not shown since we are performing an AC analysis.



$$\begin{aligned} h_{rb} &= \frac{V_{eb}}{V_{cb}} \bigg|_{I_e} = 0 \\ &= 37 \times 10^{-6} \quad \text{(Typical Value)} \\ &R_i = h_{ib} - \frac{h_{fb} \cdot h_{rb}}{h_{ob} + \frac{1}{R_L}} \\ &R_o = \frac{1}{h_{ob} - \frac{h_{fb} h_{fb}}{h_{ib} + R_S}} \\ &R_i = \frac{-h_{fb}}{h_{ib} + R_L} \\ &A_i = \frac{-h_{fb} R_L}{1 + h_{ob} R_L} \end{aligned}$$

Common Collector Amplifier

Common Collector Circuit is as shown in the Fig. The DC supply, biasing resistors and coupling capacitors are not shown since we are performing an AC analysis



The h-parameter model is shown below



Transistors at High Frequencies

At low frequencies it is assumed that transistor responds instantaneously to changes in the input voltage or current i.e., if you give AC signal between the base and emitter of a Transistor amplifier in Common Emitter configuraii6n and if the input signal frequency is low, the output at the collector will exactly follow the change in the input (amplitude etc.,). If '1' of the input is high (MHz) and the amplitude of the input signal is changing the Transistor amplifier will not be able to respond.

It is because; the carriers from the emitter side will have to be injected into the collector side. These take definite amount of time to travel from Emitter to Base, however small it may be. But if the input signal is varying at much higher speed than the actual time taken by the carries to

respond, then the Transistor amplifier will not respond instantaneously. Thus, the junction capacitances of the transistor, puts a limit to the highest frequency signal which the transistor can handle. Thus depending upon doping area of the junction etc, we have transistors which can respond in AF range and also RF range.

To study and analyze the behavior of the transistor to high frequency signals an equivalent model based upon transmission line equations will be accurate. But this model will be very complicated to analyze. So some approximations are made and the equivalent circuit is simplified. If the circuit is simplified to a great extent, it will be easy to analyze, but the results will not be accurate. If no approximations are made, the results will be accurate, but it will be difficult to analyze. The desirable features of an equivalent circuit for analysis are simplicity and accuracy. Such a circuit which is fairly simple and reasonably accurate is the Hybrid-pi or Hybrid- π model, so called because the circuit is in the form of π .

Hybrid - π Common Emitter Transconductance Model

For Transconductance amplifier circuits Common Emitter configuration is preferred. Why? Because for Common Collector (hrc< 1). For Common Collector Configuration, voltage gain Av < 1. So even by cascading you can't increase voltage gain. For Common Base, current gain is hib< 1. Overall voltage gain is less than 1. For Common Emitter, hre>>1. Therefore Voltage gain can be increased by cascading Common Emitter stage. So Common Emitter configuration is widely used. The Hybrid-x or Giacoletto Model for the Common Emitter amplifier circuit (single stage) is as shown below.



Analysis of this circuit gives satisfactory results at all frequencies not only at high frequencies but also at low frequencies. All the parameters are assumed to be independent of frequency.

WhereB' = internal node in base $r_{bb'}$ = Base spreading resistance $r_{b'e}$ = Internal base node to emitter resistance r_{ce} = collector to emitter resistance C_e = Diffusion capacitance of emitter base junction $r_{b'e}$ = Feedback resistance from internal base node to collector node g_m = Transconductance C_C = transition or space charge capacitance of base collector junction

Circuit Components

B' is the internal node of base of the Transconductance amplifier. It is not physically accessible. The base spreading resistance rbb is represented as a lumped parameter between base B and internal node B'. $g_{mVb'e}$ is a current generator. Vb'e is the input voltage across the emitter junction. If Vb'e increases, more carriers are injected into the base of the transistor. So the increase in the number of carriers is proportional to Vb'e. This results in small signal current since we are taking into account changes in Vb'e. This effect is represented by the current generator $g_mVb'e$. This represents the current that results because of the changes in Vb'e' when C is shorted to E.

When the number of carriers injected into the base increase, base recombination also increases. So this effect is taken care of by gb'e. As recombination increases, base current increases. Minority carrier storage in the base is represented by C_e the diffusion capacitance.

According to Early Effect, the change in voltage between Collector and Emitter changes the base width. Base width will be modulated according to the voltage variations between Collector and Emitter. When base width changes, the minority carrier concentration in base changes. Hence the current which is proportional to carrier concentration also changes. I_E changes and I_C changes. This feedback effect [IE on input side, I_C on output side] is taken into account by connecting gb'e between B', and C. The conductance between Collector and Base is g_{ce} .C_c represents the collector junction barrier capacitance.

Hybrid - n Parameter Values

Typical values of the hybrid-n parameter at $I_C = 1.3$ rnA are as follows:

 $g_m = 50 \text{ mA/v}$

 $rbb' = 100 \Omega$ $rb'e = 1 k\Omega$ $ree = 80 k\Omega$ Cc = 3 pfCe = 100 pf $rb'c = 4 M\Omega$

These values depend upon:

1. Temperature 2. Value of I_C

Determination of Hybrid-x Conductances

1. Trans conductance or Mutual Conductance (g_m)



The above figure shows PNP transistor amplifier in Common Emitter configuration for AC purpose, Collector is shorted to Emitter.

$$I_{\rm C} = I_{\rm C0} - \alpha_0 \ . \ I_{\rm E}$$

 I_{CO} opposes $I_E.$ I_E is negative. Hence $I_C = I_{CO} - \alpha_0 IE \; \alpha_0$ is the normal value of α at room temperature.

In the hybrid - π equivalent circuit, the short circuit current = g_mVb' e

Here only transistor is considered, and other circuit elements like resistors, capacitors etc are not considered.

$$\mathbf{g}_{\mathrm{m}} = \left. \frac{\partial \mathbf{I}_{\mathrm{C}}}{\partial \mathbf{V}_{\mathrm{b'e}}} \right|_{\mathrm{V_{\mathrm{CE}}} = \mathrm{K}}$$

Differentiate (1) with respect to Vb'e partially. I_{CO} is constant

$$g_{m} = 0 - \alpha_{0} \frac{\partial I_{E}}{\partial V_{b'e}}$$

- -

For a PNP transistor, $Vb'e = -V_E$ Since, for PNP transistor, base is n-type. So negative voltage is given

$$g_{m} = \alpha_{0} \frac{\partial I_{E}}{\partial V_{E}}$$

If the emitter diode resistance is r_e then

$$\mathbf{r}_{e} = \frac{\partial \mathbf{V}_{E}}{\partial \mathbf{I}_{E}}$$

$$g_m = \frac{\alpha_0}{r_e}$$

$$r = \frac{\eta \cdot V_T}{I} \quad \eta = 1, \qquad I = I_E \qquad r = \frac{V_T}{I_E}$$
$$g_m = \frac{\alpha_0 \cdot I_E}{V_T} \qquad \alpha_0 \simeq 1, \qquad I_E \simeq I_C$$
$$I_E = I_{C0} - I_C$$
$$g_m = \frac{I_{C0} - I_C}{V_T}$$

Neglect I_{C0}

$$\mathbf{g}_{m} = \frac{\left|\mathbf{I}_{C}\right|}{\mathbf{V}_{T}}$$

 g_m is directly proportional to I_C is also inversely proportional to T. For PNP transistor, I_C is negative

$g_m = \frac{-I_C}{V_T}$

At room temperature i.e. $T=300^{0}K$

$$g_{m} = \frac{\left|I_{C}\right|}{26}, I_{C} \text{ is in mA.}$$
If $I_{C} = 1.3 \text{ mA}, g_{m} = 0.05 \text{ A/V}$
If $I_{C} = 10 \text{ mA}, g_{m} = 400 \text{ mA/V}$

Input Conductance (gb'e):

At low frequencies, capacitive reactance will be very large and can be considered as Open circuit. So in the hybrid- π equivalent circuit which is valid at low frequencies, all the capacitances can be neglected.

The equivalent circuit is as shown in Fig.



The value of rb'c» rb'e (Since Collector Base junction is Reverse Biased)So I_b flows into rb'e only. [This is lb' (IE - I_b)will go to collector junction]

$$V_{b'e} \simeq I_{b'} r_{b'e}$$

The short circuit collector current,

$$I_{C} = g_{m} \cdot V_{b'e}; \qquad V_{b'e} = I_{b} \cdot r_{b'e}$$

$$I_{C} = g_{m} \cdot I_{b} \cdot r_{b'e}$$

$$h_{fe} = \frac{I_{C}}{I_{B}} \Big|_{V_{CE}} = g_{m} \cdot r_{b'e}$$

$$\boxed{r_{b'e} = \frac{h_{fe}}{g_{m}}}$$

$$g_{m} = \frac{|I_{C}|}{V_{T}}$$

$$r_{b'e} = \frac{h_{fe} \cdot V_{T}}{|I_{C}|}$$

$$g_{b'e} = \frac{h_{fe} \cdot V_{T}}{|I_{C}|} \text{ or } \boxed{\frac{g_{m}}{h_{fe}}}$$

.

Feedback Conductance (gb' c)

$$\label{eq:hre} \begin{split} hre = reverse \ voltage \ gain, \ with \ input \ open \ or \ I_b = 0 \\ hre = Vb'e/Vce = Input \ voltage/Output \ voltage \end{split}$$

$$h_{re} = \frac{r_{b'e}}{r_{b'e} + r_{b'c}}$$

 $[\text{With input open, i.e., } I_{b} = 0, V_{ce} \text{ is output. So it will get divided between } r_{b'e} \text{ and } r_{b'c} \text{ only}]$ or $h_{re} (r_{b'e} + r_{b'c}) = r_{b'e}$ $r_{b'e} [1 - h_{re}] = h_{re} r_{b'c}$ But $h_{re} << 1$ $\therefore \qquad r_{b'e} = h_{re} r_{b'c}; \quad r_{b'c} = \frac{r_{b'e}}{h_{re}}$ or $\frac{g_{b'c} = h_{re} g_{b'e}}{r_{b'e}} \frac{1}{r_{b'c}} = g_{b'c} = \frac{h_{re}}{r_{b'e}}$ $h_{re} = 10^{-4}$ $\therefore \qquad r_{b'c} >> r_{b'e}$

Base Spreading Resistance (r bb')

The input resistance with the output shorted is hie. If output is shorted, i.e., Collector and Emitter are joined; $r_{b'e}$ is in parallel with $r_{b'c}$.

$$h_{ie} = r_{bb'} + r_{b'e}$$

$$r_{b'e} = \frac{h_{fe} \cdot V_T}{|I_c|}$$

$$r_{bb'} = h_{ie} - r_{b'e}$$

$$h_{ie} = r_{bb'} + r_{b'e}$$

$$h_{ie} = r_{bb'} + \frac{h_{fe} \cdot V_T}{|I_c|}$$

Output Conductance (gce)

This is the conductance with input open circuited. In h-parameters it is represented as hoe. For $I_b=0$, we have,

$$\begin{split} h_{oe} &= \frac{1}{r_{ce}} + \frac{1}{r_{b'c}} + g_m \cdot h_{re} \\ &= g_{ce} + g_{b'c} + g_m \cdot h_{re} \\ g_{b'e} &= \frac{g_m}{h_{fe}} \\ g_m &= g_{b'e} \cdot h_{fe} \\ h_{re} &= \frac{r_{b'e}}{r_{b'e} + r_{b'c}} \approx \frac{r_{b'e}}{r_{b'c}} = \frac{g_{b'c}}{g_{b'e}} \\ h_{oe} &= g_{ce} + g_{b'c} + g_{b'e} \cdot h_{fe} \cdot \frac{g_{b'c}}{g_{b'e}} \\ g_{ce} &= h_{oe} - (1 + h_{fe}) \cdot g_{b'c} \\ h_{fe} &>> 1, 1 + h_{fe} \approx h_{fe} \\ \hline g_{ce} &= h_{oe} - h_{fe} \cdot g_{b'e} \\ g_{ce} &= h_{oe} - h_{fe} \cdot g_{b'e} \\ \end{split}$$

Hybrid - π Capacitances

In the hybrid - π equivalent circuit, there are two capacitances, the capacitance between the Collector Base junction is the _{Cc} or C_{b'e'}. This is measured with input open i.e., I_E = 0, and is specified by the manufacturers as C_{Ob}. 0 indicates that input is open. Collector junction is reverse biased.

$$C_C \alpha \frac{1}{(V_{CE})^n}$$

 $n = \frac{1}{2}$ for abrupt junction
= 1/3 for graded junction.

 $C_e = Emitter diffusion capacitance C_{De} + Emitter junction capacitance C_{Te}$ $C_T = Transition capacitance.$ $C_D = Diffusion capacitance.$ $C_{De} >> C_{Te}$ $C_e \simeq C_{De}$ $C_{De} \alpha I_E$ and is independent of Temperature T.

Validity of hybrid- π model

The high frequency hybrid Pi or Giacoletto model of BJT is valid for frequencies less than the unit gain frequency.

High frequency model parameters of a BJT in terms of low frequency hybrid parameters

The main advantage of high frequency model is that this model can be simplified to obtain low frequency model of BJT. This is done by eliminating capacitance's from the high frequency model so that the BJT responds without any significant delay (instantaneously) to the input signal. In practice there will be some delay between the input signal and output signal of BJT which will be very small compared to signal period (1/frequency of input signal) and hence can be neglected. The high frequency model of BJT is simplified at low frequencies and redrawn as shown in the figure below along with the small signal low frequency hybrid model of BJT.



Fig. high frequency model of BJT at low frequencies



Fig hybrid model of BJT at low frequencies

The High frequency model parameters of a BJT in terms of low frequency hybrid parameters are given below:

Transconductance $g_m = I_c/V_t$ Internal Base node to emitter resistance $r_{b'e} = h_{fe}/g_m = (h_{fe} * V_t)/I_c$ Internal Base node to collector resistance $r_{b'e} = (h_{re} * r_{b'c}) / (1 - h_{re})$ assuming $h_{re} \ll 1$ it reduces to $r_{b'e} = (h_{re} * r_{b'c})$ Base spreading resistance $r_{bb'} = h_{ie} - r_{b'e} = h_{ie} - (h_{fe} * V_t)/I_c$ Collector to emitter resistance $r_{ce} = 1 / (h_{oe} - (1 + h_{fe})/r_{b'c})$

Collector Emitter Short Circuit Current Gain

Consider a single stage Common Emitter transistor amplifier circuit. The hybrid-1t equivalent circuit is as shown:

$$I_{L} = -g_{m} V_{b'e}$$
$$V_{b'e} = \frac{I_{i}}{g_{b'e} + j\omega(C_{e} + C_{c})}$$

A, under short circuit condition is,

$$A_{1} = \frac{I_{L}}{I_{i}} = \frac{-g_{m}}{g_{b'e} + j\omega(C_{e} + C_{c})}$$
$$g_{b'e} = \frac{g_{m}}{h_{fe}}, \quad C_{e} + C_{c} \simeq C_{e}$$

$$C_{e} = \frac{g_{m}}{2\pi f_{T}}$$

$$=\frac{-g_{\rm m}}{\frac{g_{\rm m}}{h_{\rm fe}}+\frac{j\,2\pi.g_{\rm m}.f}{2\pi\,f_{\rm T}}}$$

$$\mathbf{A}_{i} = \frac{-1}{\frac{1}{\mathbf{h}_{fe}} + \mathbf{j}\left(\frac{f}{f_{T}}\right)}$$

But

...

If the output is shorted i.e. $R_L = 0$, what will be the flow response of this circuit? When $R_L = 0$, $V_o = 0$. Hence $A_v = 0$. So the gain that we consider here is the current gain I_L/I_c . The simplified equivalent circuit with output shorted is,



A current source gives sinusoidal current Ic. Output current or load current is $IL \cdot g_{b'c}$ isneglected since $g_{b'c} \ll g_{b'e}$, g_{ce} is in shunt with short circuit R = 0. Therefore g_{ce} disappears. The current is delivered to the output directly through Ce and $g_{b'c}$ is also neglected since this will be very small.

$$I_{L} = -g_{m} V_{b'e}$$

$$V_{b'e} = \frac{I_{i}}{g_{b'e} + j\omega(C_{e} + C_{c})}$$
er short circuit condition is

A, under short circuit condition is,

$$A_{i} = \frac{I_{L}}{I_{i}} = \frac{-g_{m}}{g_{b'e} + j\omega(C_{e} + C_{c})}$$
$$g_{b'e} = \frac{g_{m}}{h_{fe}}, C_{e} + C_{c} \simeq C_{e}$$
$$C_{e} = \frac{g_{m}}{2\pi f_{T}}$$

$$= \frac{\frac{-g_{\rm m}}{g_{\rm m}}}{\frac{j 2\pi g_{\rm m} f}{h_{\rm fe}}}$$

$$A_{i} = \frac{-1}{\frac{1}{h_{fe}} + j\left(\frac{f}{f_{T}}\right)}$$

But

...

$$= \frac{-h_{fe}}{1+j h_{fe} \left(\frac{f}{f_T}\right)}$$
$$A_i = \frac{-h_{fe}}{1+j \left(\frac{f}{f_\beta}\right)}$$
$$\frac{f_T}{h_{fe}} = f_\beta$$
$$|A_i| = \frac{h_{fe}}{\sqrt{1+\left(\frac{f}{f_\beta}\right)^2}}$$

Where $f_{\beta} = \frac{g_{b'e}}{2\pi (C_{e} + C_{C})}$ $g_{b'e} = \frac{g_{m}}{h_{fe}}$ $\therefore \qquad f_{\beta} = \frac{g_{m}}{h_{fe} 2\pi (Ce + C_{c})}$ $At \qquad f = f_{\beta}, \qquad A_{i} = \frac{1}{\sqrt{2}} = 0.707 \text{ of } h_{fe}.$

Current Gain with Resistance Load:

$$f_{\rm T} = f_{\beta} \cdot \mathbf{h}_{\rm fe} = \frac{\mathbf{g}_{\rm m}}{2\pi (\mathbf{C}_{\rm e} + \mathbf{C}_{\rm c})}$$

Considering the load resistance R_L

V _{b'e} is the input voltage and is equal to V_1

 $V_{ce}\,is$ the output voltage and is equal to V $_2$

$$K_2 = \frac{V_{ce}}{V_{b'e}}$$

This circuit is still complicated for analysis. Because, there are two time constants associated with the input and the other associated with the output. The output time constant will be much smaller than the input time constant. So it can be neglected.

$$\begin{split} &K = \text{Voltage gain. It will be} >> 1 \\ &g_{b'c} \left(\frac{K-1}{K}\right) \simeq g_{b'c} \\ &g_{b'c} < g_{ce} \quad \because \quad r_{b'c} \simeq 4 \text{ M}\Omega, \qquad r_{ce} = 80 \text{ K (typical values)} \end{split}$$

So $g_{b'c}$ can be neglected in the equivalent circuit. In a wide band amplifier RL will not exceed $2K\Omega$. If R_L is small f_H is large.

$$f_{\rm H} = \frac{1}{2\pi {\rm C}_{\rm S} \left({\rm R}_{\rm C} \| {\rm R}_{\rm L} \right)}$$

Therefore g_{ce} can be neglected compared with R_L . Therefore the output circuit consists of current generator gm V _{b'e} feeding the load R_L so the Circuit simplifies as shown in Fig.



$$K = \frac{V_{ce}}{V_{b'e}} = -g_m R_L; \quad g_m = 50 \text{ mA} \setminus V, \qquad R_L = 2K\Omega \text{ (typical values)}$$
$$K = -100$$

Miller's Theorem

It states that if an impedance Z is connected between the input and output terminals, of a network, between which there is voltage gain, K, the same effect can be had by removing Z and connecting an impedance Z_i at the input =Z/(1-K) and Zo across the output = ZK/(K-1)



Fig. High frequency equivalent circuit with resistive load R_L

Therefore high frequency equivalent circuit using Miller's theorem reduces to



Fig. Circuit after applying Millers' Theorem

$$K = \frac{V_{ce}}{V_{b'e}}$$

 $V_{ce}=\mbox{-} I_c$. $R_{\rm L}$

$$K = \frac{-I_{C} \cdot R_{L}}{V_{b'e}}$$
$$\frac{I_{C}}{V_{b'e}} = g_{m}$$
$$K = -g_{m} \cdot R_{L}$$

The Parameters f_T

 f_T is the frequency at which the short circuit Common Emitter current gain becomes unity.

The Parameters f_β

$$A_{i} = 1, \text{ or } \frac{h_{fe}}{\sqrt{1 + \left(\frac{f_{T}}{f_{\beta}}\right)^{2}}} = 1$$

$$f = f_{T}, A_{i} = 1$$

$$h_{fe} = \sqrt{1 + \left(\frac{f_{T}}{f_{\beta}}\right)^{2}}$$

$$(h_{fe})^{2} = 1 + \left(\frac{f_{T}}{f_{\beta}}\right)^{2} \cong \left(\frac{f_{T}}{f_{\beta}}\right)^{2}$$

$$h_{fe} \simeq \frac{f_{T}}{f_{\beta}} \text{ when } Ai = 1$$

$$\boxed{f_{T} \simeq h_{fe} \cdot f_{\beta}}$$

$$f_{\beta} = \frac{g_{m}}{h_{fe} \{C_{e} + C_{c}\}}$$

$$f_{T} = f_{\beta} \cdot h_{fe} = \frac{g_{m}}{2\pi(C_{e} + C_{c})}$$

$$\boxed{f_{T} \simeq \frac{g_{m}}{2\pi C_{e}}}$$

$$A_{i} = \frac{-g_{m}}{g_{b'e} + j\omega(C_{e} + C_{c})}$$

Dividing by gb'e' Numerator and Denominator,

$$A_{i} = \frac{-g_{m} |g_{b'e}|}{1 + \frac{j2\pi f(C_{e} + C_{c})}{g_{b'e}}}$$

we know that

...

$$\frac{g_m}{g_{b'e}} = h_{fe}$$

 $= \frac{g_m}{h_{fe}}$

 $\mathbf{g}_{b'e}$

$$A_{i} = \frac{-h_{fe}}{1 + jf\left[\frac{2\pi(C_{e} + C_{C})}{g_{b'e}}\right]}$$

ghia

But we know that $A_i = -\frac{1}{1}$ 1+ i

Comparing,

...

$$f_{\beta} = \frac{g_{b'e}}{2\pi(C_e + C_c)} = \frac{g_m}{h_{fe} \cdot 2\pi(C_e + C_c)}$$
$$f_{\beta} = \frac{g_m}{h_{fe} \cdot 2\pi(C_e + C_c)}$$
$$f_{T} = \frac{g_m}{2\pi(C_e + C_c)}$$

 $\therefore g_{b'e} = \frac{g_m}{h_{fe}}$

Gain - Bandwidth (B.W) Product

This is a measure to denote the performance of an amplifier circuit. Gain - B. W product is also referred as Figure of Merit of an amplifier. Any amplifier circuit must have large gain and large bandwidth. For certain amplifier circuits, the mid band gain Am maybe large, but not Band width or Vice - Versa. Different amplifier circuits can be compared with thus parameter.

FET: Analysis of common Source and common drain Amplifier circuits at high frequencies.

Just like for the BJT, we could use the original small signal model for low frequency analysis-the only difference was that external capacitances had to be kept in the circuit. Also just like the BJT, for high frequency operation, the internal capacitances between each of the device's terminals can no longer be ignored and the small signal model must be modified. Recall that for high frequency operation, we're stating that external capacitances are so large (in relation to the internal capacitances) that they may be considered short circuits.

High frequency response of Common source amplifier

The JFET implementation of the common-source amplifier is given to the left below, and the small signal circuit in corporating the high frequency FET model is given to the right below. As stated above, the external coupling and bypass capacitors are large enough that we can model them as short circuits for high frequencies.



We may simplify the small signal circuit by making the following approximations and observations:

1. R_{ds} is usually larger than $R_D || R_L$, so that the parallel combination is dominated by $R_D || R_L$ and r_{ds} may be neglected. If this is not the case, a single equivalent resistance, $r_{ds} || R_D || R_L$ may be defined.

2. The Miller effect transforms Cgd into separate capacitances seen in the input and output circuits as

$$C_{M1} = C_{gd} (1 - A_v) \text{ (input circuit)}$$
$$C_{M2} = C_{gd} \left(1 - \frac{1}{A_v} \right) \text{(output circuit)}^{\dagger}$$

3. Cds is very small, so the impedance contribution of this capacitance may be considered to be an open circuit and may be ignored.

$$C_{in} = C_{gs} + C_{M1} = C_{gs} + C_{gd} (1 - A_v).$$

4. The parallel capacitances in the input circuit, C_{gs} and C_{M1} , may be combined to a single equivalent capacitance of value

$$C_{in} = C_{gs} + C_{M1} = C_{gs} + C_{gd} (1 - A_v).$$

5. Similarly, the parallel capacitances in the output circuit, Cds and CM2,may be combined to a single equivalent capacitance of value

$$C_{out} = C_{ds} + C_{M2} = C_{ds} + C_{gd} \left(1 - \frac{1}{A_v} \right),$$

Where $A_V = -g_m(RD||RL)$ for a common-source amplifier.

Setting the input source, vS, equal to zero allows us to define the equivalent resistances seen by C_{in} and C_{out} (the Method of Open Circuit Time Constants).Note that, with vS=0, the dependent current source also goes to zero (opens) and the input and output circuits are separated.



 $R_{Cin} = R \mid \mid R_G$.

$$R_{Cout} = R_D || R_L$$

$$\tau_{Cin} = C_{in}R_{Cin}; \quad \tau_{Cout} = C_{out}R_{Cout},$$

$$\omega_{H} = \frac{1}{\frac{1}{\omega_{Cin}} + \frac{1}{\omega_{Cout}}} = \frac{1}{\tau_{Cin} + \tau_{Cout}} = \frac{1}{C_{in}R_{Cin} + C_{out}R_{Cout}} = \frac{1}{C_{in}(R \mid \mid R_{G}) + C_{out}(R_{D} \mid \mid R_{L})}$$

Generally, the input is going to provide the dominant pole, so the high frequency cut off is given by

$$\omega_{H} = \frac{1}{C_{in}(R \mid \mid R_{G})}; \quad f_{H} = \frac{\omega_{H}}{2\pi} = \frac{1}{2\pi C_{in}(R \mid \mid R_{G})}.$$

High frequency response of Common source amplifier



Characteristics of CDAmplifier:

- Voltagegain ≈ 1
- Highinputresistance
- Lowoutputresistance
- Goodvoltage buffer

High frequency small signal model





$$\omega_{3dB} \approx \frac{1}{R_{s} \left(\frac{C_{gs}}{1 + g_{m}R_{L}} + C_{gd} \right) + C_{db} \frac{R_{L}}{1 + g_{m}R_{L}}}$$

If R_S is not too high, bandwidth can be rather high and approach ω_T



UNIT-II

Multistage Amplifiers : Classification of amplifiers, methods of coupling, **c**ascaded transistor amplifier and its analysis, analysis of two stage RC coupled amplifier, high input resistance transistor amplifier circuits and their analysis-Darlington pair amplifier, Cascode amplifier, Bootstrap emitter follower, Analysis of multi stage amplifiers using FET, Differential amplifier using BJT.

Classification of amplifiers

Depending upon the type of coupling, the multistage amplifiers are classified as :

- 1. Resistance and Capacitance Coupled Amplifiers (RC Coupled)
- 2. Transformer Coupled Amplifiers
- 3. Direct Coupled DC Amplifiers
- 4. Tuned Circuit Amplifiers.

Based upon the B. W. of the amplifiers, they can be classified as :

- 1. Narrow hand amplifiers
- 2. Untuned amplifiers

Narrow hand amplifiers: Amplification is restricted to a narrow band of frequencies around a centre frequency. There are essentially tuned amplifiers.

Untuned amplifiers: These will have large bandwidth. Amplification is desired over a considerable range of frequency spectrum.

Untuned amplifiers are further classified w.r.t bandwidth.

I. DC amplifiers (Direct Coupled) DC to few KHz		
2. Audio frequency amplifiers (AF)	20 Hz to 20 KHz	
3. Broad band amplifier	DC to few MHz	
4. Video amplifier	100 Hz to few MHz	

The gain provided by an amplifier circuit is not the same for all frequencies because the reactance of the elements connected in the circuit and the device reactance value depend upon

the frequency. Bandwidth of an amplifier is the frequency range over which the amplifier stage gain is reasonably constant within ± 3 db, or O. 707 of A_V Max Value.

Resistance and Capacitance Coupled Amplifiers (RC Coupled)

This type of amplifier is very widely used. It is least expensive and has good frequency response. In the multistage resistive capacitor coupled amplifiers, the output of the first stage is coupled to the next through coupling capacitor and R_L . In two stages Resistor Capacitor coupled amplifiers, there is no separate R_L between collector and ground, but Reo the resistance between collector and V cc (R_C) itself acts as R_L in the AC equivalent circuit.

Transformer Coupled Amplifiers

Here the output of the amplifier is coupled to the next stage or to the load through a transformer. With this overall circuit gain will be increased and also impedance matching can be achieved. But such transformer coupled amplifiers will not have broad frequency response i.e., (f_2-f_1) is small since inductance of the transformer windings will be large. So Transformer coupling is done for power amplifier circuits, where impedance matching is critical criterion for maximum power to be delivered to the load.

Direct Coupled (DC) Amplifiers

Here DC stands for direct coupled and not (direct current). In this type, there is no reactive element. L or C used to couple the output of one stage to the other. The AC output from the collector of one stage is directly given to the base of the second stage transistor directly. So type of amplifiers is used for large amplification of DC and using low frequency signals. Resistor Capacitor coupled amplifiers cannot be used for amplifications of DC or low frequency signals since Xc the capacitive reactance of the coupling capacitor will be very large or open circuit for DC

Tuned Circuit Amplifiers

In this type there will be one RC or LC tuned circuit between collector and V_{CC} in the place of Re. These amplifiers will amplify signals of only fixed frequency.fo which is equal to the resonance frequency of the tuned circuit LC. These are also used to amplify signals of a narrow band of frequencies centered on the tuned frequency f_0 .

Distortion in Amplifiers

If the input signal is a sine wave the output should also be a true sine wave. But in all the cases it may not be so, which we characterize as distortion. Distortion can be due to the nonlinear characteristic of the device, due to operating point not being chosen properly, due to large signal swing of the input from the operating point or due to the reactive elements Land C in the circuit. Distortion is classified as:

(a) **Amplitude distortion**:

This is also called non linear distortion or harmonic distortion. This type of distortion occurs in large signal amplifiers or power amplifiers. It is due to then on linearity of the characteristic of the device. This is due to the presence of new frequency signals which are not present in the input. If the input signal is of 10 KHz the output signal should also be 10 KHz signal. But some harmonic terms will also be present. Hence the amplitude of the signal (rms value) will be different Vo = Ay Vi.

(b) Frequency distortion:

The amplification will not be the same for all frequencies. This is due to reactive component in the circuit.

(c) Phase - shift delay distortion:

There will be phase shift between the input and the output and this phase shift will not be the same for all frequency signals. It also varies with the frequency of the input signal. In the output signal, all these distortions may be present or anyone may be present because of which the amplifier response will not be good.

The performance obtainable from a single stage amplifier is often insufficient for many applications; hence several stages may be combined forming a multistage amplifier. These stages may be combined forming a multistage amplifier. These stages are connected in cascade, i.e. output of the first stage is connected to form input of second stage, whose output becomes input of third stage, and so on. The overall gain of a multistage amplifier is the product of the gains of the individual stage (ignoring potential loading effects):

Gain (A) = A1 * A2 * A3 * A4 * *An.

Alternately, if the gain of each amplifier stage is expressed in decibels (dB), the total gain is the sum of the gains of the individual stages

Gain in dB (A) = $A1 + A2 + A3 + A4 + \dots + An$.

When we want to achieve higher amplification than a single stage amplifier can offer, it is a common practice to cascade various stages of amplifiers, as it is shown in Fig.1.a. In such a structure the input performance of the resulted multistage amplifier is the input performance of the first amplifier while the output performance is that of the last amplifier. It is understood that combining amplifiers of various types we can create those characteristics that are necessary to fulfill the specifications of a specific application. In addition, using feedback techniques in properly chosen multistage amplifiers can further increase this freedom of the design.



According to the small signal equivalent circuit of a two stage amplifier shown in Fig., we can calculate the ac performance of the circuit.

Voltage amplification

$$\mathbf{A}_{v} = \frac{\mathbf{v}_{o}}{\mathbf{v}_{1}} = \frac{\mathbf{v}_{o}}{\mathbf{v}_{2}} \cdot \frac{\mathbf{v}_{o}}{\mathbf{v}_{1}} = \mathbf{A}_{v2} \cdot \mathbf{A}_{v1}$$

Current amplification

$$\mathbf{A}_{i} = \frac{\mathbf{i}_{L}}{\mathbf{i}_{s}} = \frac{\mathbf{i}_{L}}{\mathbf{i}_{2}} \cdot \frac{\mathbf{i}_{2}}{\mathbf{i}_{s}} = \mathbf{A}_{i2} \cdot \mathbf{A}_{i1}$$

Power amplification

$$\mathbf{A}_{p} = \mathbf{A}_{v} \cdot \mathbf{A}_{i} = (\mathbf{A}_{v2} \cdot \mathbf{A}_{12}) \cdot (\mathbf{A}_{v1} \cdot \mathbf{A}_{i1}) = \mathbf{A}_{p2} \cdot \mathbf{A}_{p1}$$

Cascading Transistor Amplifiers

When the amplification of a single transistor is not sufficient for a particular purpose (say to deliver output to the speaker or to drive a transducer etc) or when the input or output impedance is not of the correct magnitude for the desired application, two or more stages may be connected in cascade. Cascade means in series i.e. the output of first stage is connected to the input of the next stage.



Let us consider two stage cascaded amplifier. Let the first stage is in common emitter configuration. Current gain is high and let the II stage is in common collector configuration to provide high input impedance and low output impedance. So what are the expressions for the total current gain A_I of the entire circuit (i.e. the two stages), Z_i , A_v and Y_o ? To get these expressions, we must take the h-par ammeters of these transistors in that particular configuration. Generally manufactures specify the h-parameters for a given transistor in common emitter configuration. It is widely used circuit and also A_I is high. To get the transistor h-parameters in other configurations, converts ion formulae are used.

The Two Stage Cascaded Amplifier Circuit

The Transistor Q_1 is in Common Emitter configuration. The second Transistor Q_2 is in Common Collector (CC) configuration. Output is taken across 5K, the emitter resistance. Collector is at ground potential in the A.C. equivalent circuit. Biasing resistors are not shown since their purpose in only to provide the proper operating point and they do not affect the response of the amplifier. In the low frequency equivalent circuit, since the capacitors have large value, and so is X_c low, and can be neglected. So the capacitive reactance is not considered, and capacitive reactance X_c is low when C is large and taken as short circuit.



The small signal Common Emitter configuration circuit reduces as shown in Fig. In this circuit Q2 collector is at ground potential, in AC equivalent circuit. It is in Common Collector configuration and the output is taken between emitter point E2 and ground. So the circuit is redrawn as shown in Figure indicating voltages at different stages and input and output resistances.



Choice of Transistor in a Cascaded Amplifier Configuration

By connecting transistor in cascade, voltage gain gets multiplied. But what type of configuration should be used? Common Collector(CC) or Common Base(CB) or Common
Emitter(CE)? To get voltage amplification and current amplification, only Common Emitter (CE) configuration is used. Since it is Common Collector amplifier, the voltage gain is less than one for each stage. So the overall amplification is less than 1.

Common Base Configuration is also not used since A₁ is less than 1.

$$A_V = A_I \times \frac{R_L}{R_i}$$

Effective load resistance R_L is parallel combination of R_c and R_i of the following stage, (next stage) (since in multi stage connection, the output of one stage is the input to the other stage). This parallel combination is less than R_i . Therefore $R_L/R_i < 1$.

The current gain A_I in common base configurations is hib< 1 or =1.Therefore overall voltage gain = 1. Therefore Common Base configuration is not used for cascading. So only Common Emitter configuration is used (hfe>> I).Therefore overall voltage gain and current gains are> 1 in Common Emitter configuration.

Two stage RC coupled amplifier

One way to connect various stages of a multistage amplifier is via capacitors, as indicated in the two-stage amplifier in Figure. Where two stages of common emitter amplifier are coupled to each other by the capacitor C_3 .



In RC-coupled amplifiers:

1. The various stages are DC isolated. This feature facilitates the biasing of individual stages.

2. The various stages can be similar. Hence the design of the amplifier is simplified.

- 3. The coupling capacitors influence the responses of the amplifier.
- 4. A great number of biasing resistors is necessary.



The most commonly used coupling in amplifiers is RC coupling. An RC-coupling network is shown in the illustration above. The network of R1, R2, and C1 enclosed in the dashed lines of the figure is the coupling network. You may notice that the circuitry for Q1 and Q2 is incomplete. That is intentional so that you can concentrate on the coupling network. R1 acts as a load resistor for Q1 (the first stage) and develops the output signal of that stage. Do you remember how a capacitor reacts to ac and dc? The capacitor, C1, "blocks" the dc of Q1's collector, but "passes" the ac output signal. R2 develops this passed, or coupled, signal as the input signal to Q2 (the second stage). This arrangement allows the coupling of the signal while it isolates the biasing of each stage. This solves many of the problems associated with direct coupling.

CE - CC Amplifiers

This is another type of two-stage BJT amplifier. The first stage in Common Emitter (CE) configuration provides voltage and current gains. The second stage in Common-Collector (CC) configuration provides impedance matching. This circuit is used in audio frequency amplifiers. The circuit is shown in Fig.



$$A_{V} = A_{V_{1}} \cdot A'_{V_{2}}$$
$$R_{i} = R_{i_{1}}$$
$$R_{ij} = R_{0_{1}}$$
$$A_{I} = \frac{A_{V} \cdot R_{i_{1}}}{R_{L_{2}}}$$

High Input Resistance Transistor Circuits

In some applications the amplifier circuit will have to have very high input impedance. Common Collector Amplifier circuit has high input impedance and low output impedance. But it's $A_v < 1$.If the input impedance of the amplifier circuit is to be only 500 KO or less the Common Collector Configuration can be used. But if still higher input impedance is required a circuit. This circuit is known as the Darlington Connection (named after Darlington) or Darlington Pair Circuit.

The Darlington Pair

This is two transistors connected together so that the amplified current from the first is amplified further by the second transistor. This gives the Darlington pair a very high current gain such as 10000. Darlington pairs are sold as complete packages containing the two transistors. They have three leads (B, C and E) which are equivalent to the leads of a standard individual transistor.



In this circuit, the two transistors are in Common Collector Configuration. The output of the first transistor Q_1 (taken from the emitter of the Q_1) is the input to the second transistor Q_2 at

the base. The input resistance of the second transistor constitutes the emitter load of the first transistor. So, Darlington Circuit is nothing but two transistors in Common Collector Configuration connected in series. The same circuit can be redrawn as AC equivalent circuit. So, DC is taken as ground shown in below Fig. Hence 'C' at ground potential, Collectors of transistors Q_1 and Q_2 is at ground potential.



There is no resistor connected between the emitter of Q_1 and ground i.e., Collector Point. So, we can assume that infinite resistance is connected between emitter and collector.



The overall current gain is equal to the two individual gains multiplied together:

Darlington pair current gain, $h_{FE} = h_{FE1} \times h_{FE2}$

Here h_{FE1} and h_{FE2} are the gains of the individual transistors

If both the transistors are identical then

Current gain

$$A_{I} = \frac{I_{c}}{I_{b_{I}}} \cong (h_{fe})^{2}$$

Input resistance

$$\mathbf{R}_{i} \simeq \frac{\left(\mathbf{l} + \mathbf{h}_{fe}\right)^{2} \mathbf{R}_{e}}{\mathbf{l} + \mathbf{h}_{oe} \mathbf{h}_{fe} \mathbf{R}_{e}}$$

Voltage gain

$$A_v \cong \left(1 - \frac{h_{ie}}{Ri_2}\right)$$

Output resistance

$$R_{o2} = \frac{R_{s} + h_{ie}}{(1 + h_{fe})^{2}} + \frac{h_{ie}}{1 + h_{fe}}$$

Therefore, the characteristic of Darlington Circuit are

- 1. Very High Input Resistance
- 2. Very Large Current Gain
- 3. Very Low Output Resistance
- 4. Voltage Gain, $A_v < 1$.

This gives the Darlington pair a very high current gain, such as 10000, so that only a tiny base current is required to make the pair switch on.

A Darlington pair behaves like a single transistor with a very high current gain. It has three leads (B, C and E) which are equivalent to the leads of a standard individual transistor. To turn on there must be 0.7V across both the base-emitter junctions which are connected in series inside the Darlington pair, therefore it requires 1.4V to turn on.

Darlington pairs are available as complete packages but you can make up your own from two transistors; TR1 can be a low power type, but normally TR2 will need to be high power. The maximum collector current Ic(max) for the pair is the same as Ic(max) for TR2.

A Darlington pair is sufficiently sensitive to respond to the small current passed by your skin and it can be used to make a touch-switch as shown in the diagram. For this circuit which just lights an LED the two transistors can be any general purpose low power transistors. The 100k resistor protects the transistors if the contacts are linked with a piece of wire. Two transistors may be combined to form a configuration known as the Darlington pair which behaves like a single transistor with a current gain equivalent to the product of the current gain of the two transistors. This is especially useful where very high currents need to be controlled as in a power amplifier or power-regulator circuit. Darlington transistors are available whereby two transistors are combined in one single package. The base-emitter volt-drop is twice that of a small transistor.

Disadvantages

1. The h-parameters for both the transistors will not be the same.

2. Leakage Current is more

The CASCODE Transistor Configuration

The circuit is shown in Figure. This transistor configuration consists of a Common Emitter Stage in cascade with a Common Base Stage. The collector current of transistor Q) equals the emitter current of Q_2 .

The transistor Q_1 is in Common Emitter Configuration and transistor Q_2 is in Common Base Configuration. Let us consider the input impedance (h₁₁) etc., output admittance (h₂₂) i.e. the h - parameters of the entire circuit in terms of the h- parameters of the two transistors



Input impedance

$$h_{11} = \text{Input } Z = \left. \frac{V_1}{I_1} \right|_{V_2 = 0}$$

 $h_{11} \cong h_{10}$

Short circuit current gain

$$\begin{split} h_{21} &= \frac{I_2}{I_1} \bigg|_{V_2 = 0} \\ h_{21} &= \frac{I_2}{I_1} = \frac{I}{I_1} \times \frac{I_2}{I_0} \bigg|_{V_2 = 0} \\ \frac{I'}{I_1} &= h_{fe} \qquad \text{since, } I = I_{C_1} \cdot I_1 = I_{B_1} \\ \frac{I_2}{I'} &= -h_{fb} \qquad \text{since, } I = I_{E_2} \cdot I_2 = I_{C_2} \cdot \\ h_{21} &= -h_{fe} \cdot h_{fb} \cdot \\ h_{fe} &>> 1 \cdot -h_{fb} \simeq 1, \qquad \text{since } h_{fb} = \frac{I_C}{I_E} \end{split}$$

Output conductance

$$h_{22} = \frac{I_2}{V_2}\Big|_{I_1 = 0}$$

Reverse voltage gain

.

$$h_{12} = \frac{V_1}{V_2} \Big|_{I_1 = 0}$$
$$= \frac{V_1}{V'} \times \frac{V^1}{V_2} \Big|_{I_1 = 0}$$
$$\frac{V_1}{V_0'} \Big|_{I_1 = 0} = h_{re} \cdot \frac{V'}{V_2} \Big| = h_{rb}$$

$h_{12} \cong h_{re} h_{rb}$.	
$h_{re} \simeq 10^{-4}$ $h_{rb} \simeq$	10 ⁻⁴ . ∵ h ₁₂ is very small
$h_i = h_{11} \cong h_{ie}$.	Typical value = $1.1K\Omega$
$h_f = h_{21} \cong h_{fe}.$	Typical value = 50
$h_o = h_{22} \cong h_{ob}$.	Typical value = 0.49 μ A/V
$h_r = h_{12} \cong h_{re} h_{rb}$	Typical value = 7×10^{-8} .

Therefore, for a CASCODE Transistor Configuration, its input Z is equal to that of a single Common Emitter Transistor (hie)' Its Current Gain is equal to that of a single Common Base Transistor (h_{fe}). Its output resistance is equal to that of a single Common Base Transistor (hob)' the reverse voltage gain is very small, i.e., there is no link between V $_1$ (input voltage) and V₂ (output voltage). In other words, there is negligible internal feedback in the case of, a CASCODE Transistor Circuit, acts like a single stage C.E. Transistor (Since hie and hfe are same) with negligible internal feedback (:.hre is very small) and very small output conductance, (= hob) or large output resistance (= $2M\Omega$ equal to that of a Common Base Stage). The above values are correct, if we make the assumption that hob $R_L < 0.1$ or RL is <200K.

CASCODE Amplifier will have

- 1. Very Large Voltage Gain.
- 2. Large Current Gain
- 3. Very High Output Resistance.

Boot-strap emitter follower

The maximum input resistance of a practical Darlington Circuit is only 2 M Ω . Higher input resistance cannot be achieved because of the biasing resistors R₁, R₂ etc. They come in parallel with R_i of the transistors and thus reduce the value of Ri. The maximum value of Ri is only 1/hob since, hob is resistance between base and collector. The input resistance can be increased greatly by boot strapping, the Darlington Circuit through the addition of Co between the first collector C₁ and emitter B₂.



In Fig, V is an AC signal generator, supplying current I to R. Therefore, the input resistance of V seen by the generator is $R_1 = V/I = R$ itself. Now suppose, the bottom end of R is not at ground potential but at higher potential i.e. another voltage source of KV (K < I) is connected between the bottom end of R and ground. Now the input resistance of the circuit is

$$R'_{i} = \frac{V}{I'} \qquad I' = \frac{(V - KV)}{R}$$
$$R'_{i} = \frac{VR}{V(1 - K)} = \frac{R}{1 - K}$$



I' can be increased by increasing V. When V increases KV also increases. K is constant. Therefore the potential at the two ends of R will increase by the same amount, K is less than 1, therefore $R_i > R$. Now if K = 1, there is no current flowing through R (So V = KV there is nopotential difference). So the input resistance R = 00. Both the top and bottom of the resistorterminals are at the same potential. This is called as the Boots Strapping method which increases theinput resistance of a circuit. If the potential at one end of the resistance changes, the other end of Ralso moves through the same potential difference. It is as if R is pulling itself up by its boot straps. For CC amplifiers $A_v < 1 = 0.095$. So R_i can be made very large by this technique. K = Av = 1. If we pull the boot with both the edges of the strap (wire) the boot lifts up. Here also, if the potential one end of R is changed, the voltage at the other end also changes or the potential level of R_3 rises, as if it is being pulled up from both the ends.

$$R_{i} = \frac{h_{ie}}{1 - A_{V}}; \quad A_{V} \cong 1.$$
$$R_{i} = \frac{R}{1 - K}$$

AC Equivalent circuit



Two Stage RC Coupled JFET amplifier (in Common Source (CS) configuration)

The circuit for two stages of RC coupled amplifier in CS configuration is as shown in fig.



The output Vo of I Stage is coupled to the input Vi of II Stage through a blocking capacitor C_b . It blocks the DC components present in the output or I Stage from reaching the input of the I stage which will alter the biasing already fixed for the active device. Resistor Rg is connected between gate and ground resistor Ro is connected between drain and V_{DD} supply. C_S is the bypass capacitor used to prevent loss of gain due to negative feedback. The active device is assumed to operate in the linear region. So the small signal model of the device is valid. Frequency Roll-off is the term used for the decrease in gain with frequency in the uppercut-off region. It is expressed as db/octave on db/decade.

The purpose of multistage amplifiers is to get large .gain. So with BJTs, Common Emitter Configuration is used. If JFETs are employed, common source configuration is used.

UNIT III FET Biasing AND FET Amplifiers

FET-Biasing and FET Amplifiers: FET biasing: fixed bias and self bias. FET Amplifiers: Analysis of Common source (C.S), Common Drain (C.D) JFET Amplifiers, comparison of performance with BJT Amplifiers,

BIASING FET:-

For the proper functioning of a linear FET amplifier, it is necessary to maintain the operating point Q stable in the central portion of the pinch off region The Q point should be independent of device parameter variations and ambient temperature variations

Thiscanbeachievedbysuitablyselectingthegateto sourcevoltageVGSand draincurrentID which is referred to as biasing

JFET biasing circuits are very similar to BJT biasing circuits The main difference betweenJFETcircuitsandBJTcircuitsistheoperationoftheactivecomponentsthemselves

TherearemainlytwotypesofBiasingcircuits

- 1) Selfbias
- 2) Voltagedivider-bias.

SELFBIAS

Self bias is a JFET biasing circuit that uses a source resistor to help reverse bias the JFET gate. A self bias circuit is shown in the fig. Self bias is the most common type of JFET bias. This JFET must be operated such that gate source junction is always reverse biased. This condition requires a negative VGS for an N channel JFET and a positive VGS for P channel JFET. This can be achieved using theself biasarrangementasshowninFig.ThegateresistorRG doesn'taffectthe biasbecauseithasessentially no voltage drop across it, and: the gate remains at OV .RG is necessary only to isolate an ac signal from ground in amplifier applications. The voltage drop across resistor RS makes gate sourcejunction reverse biased.



Forthedcanalysiscouplingcapacitorsareopencircuits. For

the N channel FET in Fig (a)

IS produces a voltage drop across RS and makes the source positive w.r.t ground. In any JFET circuit all the source current passes through the device to the drain circuit .This is due to the fact that there is no significant gate current.

Wecan definesourcecurrentasIS=ID

(VG=0because there is no gate current flowing in RGSoVG across RG is zero) VG = 0

then VS= ISRS = ID RS

VGS=VG-VS=0-IDRS=-IDRS

DCanalysis ofselfBias:-

 $In the following {\sf DC} analysis, the {\sf N} channel {\sf JFET} shown in the fig. is used for illustration.$

ForDCanalysiswecanreplacecoupling capacitorsbyopencircuitsandwecanalsoreplacethe resistor RG by a short circuit equivalent.:. IG = 0.The relationbetweenID and VGS is given by



Id=Idss $[1 - \frac{Vgs}{v_m}]^2$ VGSforNchannel JFET is=-idRs

Substutingthisvalueintheaboveequation

 $Id=Idss[1-\frac{(-IdRs)}{Vp}]^2$ $Id=Idss[1+\frac{(IdRs)}{Vp}]^2$

FortheN-chanelFETintheabovefigure

Is produces a voltage drop across Rs and makes the source positive w.r.t ground in any JFET circuit all the source current passes through the device to drain circuit this is due to the fact that there is no significant gate current. Therefore we can define source current as Is=Id andVg=0 then

Vs=Is Rs =IdRs

Vgs=Vg-Vs=0-IdRs=-IdRs

Drawingtheselfbiasline:-

TypicaltransfercharacteristicsforaselfbiasedJFETareshowninthefig.

Themaximum draincurrent is5mAandthegatesource cutoffvoltageis -3V.Thismeansthegate voltage has to be between 0 and -3V.



Now using the equation VGS = -IDRS and assuming RSofany suitable value we can draw the selfbias line.

Letusassume RS=500Ω

WiththisRs,wecanplottwopointscorrespondingtoID=0andId=IDSS for ID =0

VGS=-IDRS

VGS=0X(500.Ω)=0V

Sothefirstpointis(0,0)

(I_d,VGS)

ForID= IDSS=5mA

VGS=(-5mA)(500Ω) =-3V

Sothe2ndPointwillbe (5mA,-3V)

By plotting these two points, we can draw the straight line through the points. This line will intersect the transconductance curve and it is known as self bias line. The intersection point gives the operating point of the self bias JFET for the circuit.

At Q point ,the ID is slightly > than2mA and VGS is slightly > -1V. The Q point forthe self bias JFET depends on the value of Rs.If Rs is large, Q point far down on the transconductance curve ,ID is small,when Rs is small Q point is far up on the curve ,ID is large.

VOLTAGEDIVIDERBIAS:-



The fig. shows N channel JFET with voltage divider bias. The voltage at the source of JFET must be more positive than the voltage at the gate in order to keep the gate to source junction reverse biased. The source voltage is

VS=IDRS

The gate voltage is set by resistors R1 and R2 as expressed by the following equation using the voltage divider formula.

$$Vg = \left(\frac{R2}{(R1+R2)}\right) Vdd$$

Fordcanalysis



ApplyingKVLtotheinputcircuit

VG-VGS-VS =0

::VGS=VG-Vs=VG-ISRS

VGS=VG-IDRS ::IS=ID

ApplyingKVLtotheinputcircuitweget

VDS+IDRD+VS-VDD =0

::VDS=VDD-IDRD-IDRS

VDS = VDD-ID (RD + RS)

TheQpoint ofaJFETamplifier, using the voltaged ivider bias is IDQ =

IDSS[1-VGS/VP]2

VDSQ=VDD-ID(RD+RS)

COMPARISONOFMOSFETWITHJFET

- a. Inenhancementand depletion types of MOSFET, the transverse electric field induced across an insulating layer deposited on the semiconductor material controls the conductivity of the channel.
- b. IntheJFETthetransverseelectricfieldacrossthereversebiasedPNjunctioncontrols the conductivity of thechannel.

- c. The gate leakage current in a MOSFET is of the order of 10^{-12} A. Hence the input resistance of a MOSFET is very high in the order of 10^{10} to 10^{15} Ω . The gate leakage current of a JFET is of the order of 10^{-9} A., and its input resistance is of the order of 10^{8} Ω .
- d. TheoutputcharacteristicsoftheJFETareflatterthanthoseoftheMOSFET, and hence the drain resistance of aJFET (0.1to $1M\Omega$) is much higher than that of a MOSFET (1 to $50k\Omega$).
- e. JFETsareoperatedonly inthedepletionmode.ThedepletiontypeMOSFETmaybe operated in both depletion and enhancementmode.
- f. ComparingtoJFET,MOSFETsareeasiertofabricate.
- g. SpecialdigitalCMOScircuitsareavailablewhichinvolvenearzeropowerdissipationand very low voltage and current requirements. This makes them suitable for portable systems.

FETAMPLIFIERS

INTRODUCTION

Field Effect Transistor (FET) amplifiers provide an excellent voltage gain and high input impedence.Becauseofhighinput impedenceandothercharacteristics of JFETsthey are preferred over BJTs for certain types of applications.

Thereare3basicFETcircuitconfigurations:

i) CommonSource

- ii) CommonDrain
- iii) CommonGain

SimilartoBJTCE,CCandCBcircuits,only differenceisinBJTlargeoutputcollectorcurrentis controlledbysmallinputbasecurrentwhereasFETcontrolsoutputcurrentbymeansofsmallinputvoltage. In both the cases output current is controlledvariable.

FETamplifiercircuitsusevoltagecontrollednatureoftheJFET.InPinchoffregion,I_Ddepends only on

V_{GS}.

CommonSource(CS)Amplifier



Fig. 5.1(a) CSAmplifier (b) Small-signal equivalent circuit

Asimple CommonSourceamplifier isshown inFig.5.1(a) and associated small signal equivalent circuit using voltage-source model of FET is shown in Fig. 5.1(b)

VoltageGain

Source resistance(R_s)isusedtosettheQ-PointbutisbypassedbyC_sformid-frequency operation.

From the small signal equivalent circuit, the output voltage Vo = -

 $R_D \mu V_{gs}(R_D + r_d)$

Where V_{gs} =V_i,the inputvoltage, Hence,

the voltage gain,

 $A_V = V_O / V_i = -R_D \mu (R_D + r_d)$

InputImpedence

FromFig.5.1(b)InputImpedenceis Z_i =

 \mathbf{R}_{G}

ForvoltagedividerbiasasinCEAmplifiersof BJT

 $R_G = R_1 \| R_2$

Output Impedance

Output impedance is the impedance measured at the output terminals with the input voltage $V_i = 0$ From the Fig. 5.1(b) when the input voltage $V_i = 0$, $V_{gs} = 0$ and hence

 $\mu V_{gs}=0$

The equivalent circuit for calculating output impedence is given in Fig. 5.2. Output

impedence $Z_o = r_d \| R_D$

Normallyr_dwill befargreaterthan R_D . Hence $Z_0 \approx R_D$

Common Drain Amplifier

A simple common drain amplifier is shown in Fig. 5.2(a) and associated small signal equivalent circuit using the voltage source model of FET is shown in Fig. 5.2(b). Since voltage V_{gd} is more asily determined than V_{gs} , the voltage source in the output circuit is expressed in terms of V_{gs} and Thevenin's theorem.



Fig. 5.2(a) CDAmplifier (b) Small-signal equivalent circuit



Theoutputvoltage,

 $V_{O} = R_{S} \mu V_{gd} / (\mu + 1) R_{S} +$

 r_d Where $V_{gd} = V_i$ the input voltage.

Hence, the voltage gain,

 $A_v=V_O/V_i=R_S\mu/(\mu+1)R_S+r_d$

InputImpedence

FromFig.5.2(b),InputImpedence Z_i=R_G

Output Impedence

FromFig.5.2(b),Output impedence measuredattheoutputterminalswithinputvoltageVi=Ocanbe calculated

from the following equivalent circuit.

As $V_i=0$: $V_{gd}=0$: $\mu v_{gd}/(\mu + 1)=0$ Output

Impedence

 $Z_0 = r_d / (\mu + 1) \| R_s$

Whenµ»1

 $Z_{O}=(r_{d}/\mu) \| R_{S}=(1/g_{m}) \| R_{S}$

BIASINGFET

For the proper functioning of a linear FET amplifier, it is necessary to maintain the operating point Q stable in the central portion of the pinch off region The Q point should be independent of device parameter variations and ambient temperature variations

This can be achieved by suitably selecting the gate to source voltage VGS and drain current ID which is referred to as biasing

JFETbiasingcircuitsareverysimilartoBJTbiasing circuitsThemaindifferencebetweenJFET circuits and BJT circuits is the operation of the active components themselves

TherearemainlytwotypesofBiasingcircuits

- 1. Selfbias
- 2. Voltagedividerbias.

5.13.1.SELFBIAS:-

 ${\it Selfbias is a JFET bias ingcircuit that uses a source resistor to help reverse bias the JFET gate.$

Aselfbiascircuitisshowninthefig5.3



SelfbiasisthemostcommontypeofJFETbias.

ThisJFETmustbe operated such that gates our cejunction is always reverse biased.

ThisconditionrequiresanegativeVGSforanNchannelJFETandapositiveVGSforPchannelJFET. This can be achieved using the self bias arrangement as shown in Fig 5.3.

ThegateresistorRGdoesn'taffectthebiasbecause ithasessentiallynovoltagedropacrossit, and:

thegateremainsatOV.RGisnecessaryonlytoisolate anacsignalfromgroundinamplifierapplications. The voltage drop across resistor RS makes gate source junction reverse biased.

DC analysis of self Bias:-

InthefollowingDCanalysis, the Nchannel JFET shown in the fig 5.4. is used for illustration.

ForDCanalysiswecanreplacecouplingcapacitorsbyopencircuitsand we canalsoreplace the resistor RG by a short circuitequivalent.

:.IG= 0

TherelationbetweenIDandVGSisgivenby

$$[d=Idss[1-\frac{Vgs}{Vp}]^2$$

	∮ V _{DD}	
activities must be open 1000, require		
nne Re does kontone the g and in angli	R _S V _S	e giù a constan on voltan da bolate a a n

VGS for N channel JFET is =-id Rs

Substutingthisvalueintheaboveequation

 $Id=Idss[1-\frac{(-IdRs)}{Vp}]^2$

 $Id=Idss[1+\frac{(IdRs)}{v_m}]^2$ FortheN-chanelFETintheabovefigure

 $\label{eq:starses} Is produces a voltaged rop across Rs and makes the source positive w.r.t ground$

inanyJFETcircuitallthe source currentpassesthroughthedevicetodraincircuitthisisduetothe fact that there is no significant gate current

thereforewecandefinesourcecurrentasIs=IdandVg=Othen Vs= Is

Rs =IdRs

Vgs=Vg-Vs=0-IdRs=-IdRs

Drawingtheselfbiasline:-

TypicaltransfercharacteristicsforaselfbiasedJFETareshowninthefigure5.5below:

Themaximum draincurrent is6mAandthegatesource cutoffvoltageis -3V.Thismeansthegate voltage has to be between 0 and -3V.



Now using the equation VGS = -IDRS and assuming RSofany suitable value we can draw theselfbias line.

LetusassumeRS=500Ω

With this Rs , we can plot two points corresponding to ID =0 and Id=IDSS for

ID =0

VGS=-IDRS

VGS=0X(500.Ω)=0V

Sothefirstpointis(0,0)

(I_d,VGS)

ForID= IDSS=6mA

VGS=(-6mA)(500Ω)=-3V

Sothe2ndPointwillbe (6mA,-3V)

By plotting these two points, we can draw the straight line through the points. This line will intersect the transconductance curve and it is known as self bias line. The intersection point gives the operating point of the self bias JFET for the circuit.

At Q point ,the ID is slightly > than 2mA and VGS is slightly > -1V. The Q point for the selfbias JFET depends on the value of Rs.If Rs is large, Q point far down on the transconductance curve ,ID is small,when Rs is small Q point is farup on the curve ,ID is large.



The fig5.6 shows N channel JFET with voltage divider bias. The voltage at the source of JFET mustbemore positive than thevoltageatthe gatein order to keep thegateto sourcejunction reverse biased. The source voltage is

VS=IDRS

The gate voltage is set by resistors R1 and R2 as expressed by the following equation using the voltage divider formula.

Vg=

 \sqrt{dd}

5.13.2VOLTAGEDIVIDERBIAS:-

Fordcanalysisfig5.5



ApplyingKVLtotheinputcircuit

VG-VGS-VS =0

::VGS=VG-Vs=VG-ISRS

VGS=VG-IDRS ::IS=ID

ApplyingKVLtotheinputcircuitweget

VDS+IDRD+VS-VDD =0

::VDS=VDD-IDRD-IDRS

VDS = VDD-ID (RD +RS)

TheQpoint ofaJFETamplifier, using the voltage divider bias is IDQ = IDSS[1-

VGS/VP]2

VDSQ=VDD-ID(RD+RS)

UNITIV FEEDBACK AMPLIFIERS

Concept of Feedback and types, Effects of negative feedback on amplifiers characteristics, voltage series, current series, current shunt, and voltage shunt feedback amplifiers.

A practical amplifier has a gain of nearly one million *i.e.* its output is one million times the input. Consequently, even a casual disturbance at the input will appear in the amplified form in the output. There is a strong tendency in amplifiers to introduce *hum* due tosudden temperature changes or stray electric and magnetic fields. Therefore, every high gain amplifier tends to give noise along with signal in its output. The noise in the output of an amplifier is undesirable and must be kept to as small a level as possible. The noise level in amplifiers can be reduced considerably by the use of *negative feedback i.e.* by injecting a fraction of output in phase opposition to the input signal. The object of this chapter is to consider the effects and methods of providing negative feedback in transistoramplifiers.

Ideally an amplifiershould reproduce the input signal, with change in magnitude and withorwithoutchangeinphase. But some of the shortcomings of the amplifier circuit are

- 1. Changeinthevalueofthegainduetovariation insupplyingvoltage,temperature or due tocomponents.
- 2. Distortioninwave-formduetononlinearitiesintheoperatingcharacters of the Amplifying device.
- 3. The amplifier may introduce noise (undesired signals)

 $\label{eq:theta} The above drawback scan be minimizing if we introduce feedback.$

CLASSIFICATIONOFAMPLIFIERS

Amplifierscanbeclassifiedbroadlyas:

- 1. Voltage amplifiers.
- 2. Currentamplifiers.
- 3. Tranconductanceamplifiers.
- 4. Tranresistanceamplifiers.







represent the open circuit voltage gain.

1.2 Current amplifier



if
$$R_i << R_s$$

then $I_i \approx I_s$
and if $R_o >> R_L$
then
 $I_o \approx A_i I_i \approx A_i I_s$
hence $A_i \equiv \frac{I_o}{I_i}$
with $R_r = 0$

represent the short circuit current gain.

1.3 Transconductance amplifier





represent the short circuit mutual or transfer conductance

1.4 Transresistance amplifier



 $\quad \text{if} \quad R_i << R_s$

then
$$I_i \approx I_s$$

and if $R_o << R_L$ then

$$\frac{V_o \approx R_m I_i \approx R_m i_s}{\text{hence} \ R_m \equiv \frac{V_o}{I_i}}$$

with $R_L = \infty$

represent the open circuit mutual or transfer resistance.

ConceptofFeedback

An amplifier circuit simply increases the signal strength. But while amplifying, it just increases the strength of its input signal whether it contains information or some noise along withinformation. This noiseorsomedisturbance is introduced in the amplifiers becauseoftheir strong tendency to introduce hum due to sudden temperature changes or stray electric and magnetic fields. Therefore, every high gain amplifier tends to give noise along with signal in its output, which is very undesirable.

The noise level in the amplifier circuits can be considerably reduced by using negative feedback done by injecting afractionofoutput in phase opposition to the input signal.

PrincipleofFeedbackAmplifier

Afeedbackamplifiergenerallyconsistsoftwoparts.Theyaretheamplifier and the feedback circuit. The feedback circuit usually consists of resistors. The concept of feedback amplifier can be understood from the following figure.

From the above figure, the gain of the amplifier is represented as A. the gain of the amplifier is the ratio of output voltage V_o to the input voltage V_i . the feedback network extractsavoltage $V_f = \beta V_o$ from the output V_o of the amplifier.

This voltage is added for positive feedback and subtracted for negative feedback, from the signal voltage V_s. Now,

Vi=Vs+Vf=Vs+βVo Vi=Vs-Vf=Vs-βVo

The quantity $\beta = V_f / V_o$ is called as feedback ratio or feedback fraction.

Let us consider the case of negative feedback. The output V_omust be equal to the input voltage (V_s- β V_o) multiplied by the gain A of the amplifier.

Hence,

 $(V_{s}-\beta V_{o})A=V_{o}$ Or $AV_{s}-A\beta V_{o}=V_{o}$ Or $AV_{s}=V_{o}(1+A\beta)$ Therefore, $\frac{Vo}{Vs} = \frac{A}{1+A\beta}$

Let A_f be the overall gain (gain with the feedback) of the amplifier. This is defined as the ratio of output voltage V_0 to the applied signal voltage V_s , i.e.,

Af=

The equation of gain of the feedback amplifier, with positive feedback is given by

$$Af = \frac{A}{1 - A\beta}$$

A

 $1+A\beta$

These are the standard equations to calculate the gain offeed back amplifiers.

TypesofFeedbacks

The process of injecting a fraction of output energy of some device back to the input is knownas Feedback. It has beenfoundthat feedback is very useful inreducing noise and making the amplifier operation stable.

Depending upon whether the feedback signal aids or opposes the input signal, there are two types of feedbacks used.

PositiveFeedback

Thefeedbackinwhichthefeedback energyi.e., eithervoltageorcurrentis inphasewith the input signal and thus aids it is called asPositive feedback.

Boththeinputsignalandfeedbacksignalintroducesaphaseshiftof180°thusmakinga 360°resultant phaseshift around the loop, tobe finally inphase with the inputsignal.

Thoughthepositivefeedbackincreasesthegainoftheamplifier, it has the disadvantages such as

- Increasing distortion
- Instability

It is because of these disadvantages the positive feedback is not recommended for the amplifiers. If the positive feedback is sufficiently large, it leadstoos cillations, by which oscillator circuits are formed.

NegativeFeedback

The feedback in which the feedback energy i.e., either voltage or current is out of phase with the input and thus opposes it, is called as negative feedback.

In negative feedback, the amplifier introduces aphase shift of 180° into the circuit while thefeedback network issodesignedthat it producesnophaseshiftorzerophaseshift. Thusthe resultant feedback voltage V_f is 180° out of phase with the input signalV_{in}.

Though the gain of negative feedback amplifier is reduced, there are many advantages of negative feedback such as

- Stabilityofgainisimproved
- Reductionindistortion
- Reductioninnoise
- Increaseininputimpedance
- Decreaseinoutputimpedance
- Increaseintherangeofuniformapplication

 $\label{eq:lisbecause} It is because of these advantages negative feedback is frequently employed in amplifiers.$

Negative feedback in an amplifier is the method of feeding a portion of the amplified outputtothe inputbut inoppositephase. The phase opposition occurs as the amplifier provides 180° phase shift whereas the feedback network doesn't.

While the output energy is being applied to the input, for the voltage energy to be taken as feedback, the output is taken in shunt connection and for the current energy to be taken as feedback, the output is taken in series connection.

Therearetwomaintypesofnegativefeedbackcircuits. They are-

- NegativeVoltageFeedback
- NegativeCurrentFeedback

NegativeVoltageFeedback

Inthismethod, the voltage feedback to the input of amplifier is proportional to the output voltage. This is further classified into two types –

- Voltage-seriesfeedback
- Voltage-shuntfeedback

NegativeCurrentFeedback

Inthismethod, the voltage feedback to the input of amplifier is proportional to the output current. This is further classified into two types.

- Current-seriesfeedback
- Current-shunt feedback

Letushaveabriefideaonallofthem.

Voltage-Series Feedback

Inthevoltageseriesfeedbackcircuit, a fraction of the output voltage is applied inseries with the input voltage through the feedback circuit. This is also known as shunt-driven series - fed feedback, i.e., a parallel-series circuit.

The following figure shows the block diagram of voltage series feedback, by which it is evidentthatthefeedbackcircuit isplacedinshuntwiththeoutputbut inseries withtheinput.



As the feedback circuit is connected in shunt with the output, the output impedance is decreased and due to the series connection with the input, the input impedance is increased.

Voltage-ShuntFeedback

In the voltage shunt feedback circuit, a fraction of the output voltage is applied in parallel with the input voltage through the feedback network. This is also known as shunt-driven shunt-fed feedbacki.e., a parallel-parallel proto type.

The below figure shows the block diagram ofvoltage shunt feedback,by whichit is evident that the feedback circuit is placed in shunt with the output and also with the input.



As the feedback circuit is connected in shunt with the output and the input as well, both the output impedance and the input impedance are decreased.

Current-SeriesFeedback

In the current series feedback circuit, a fraction of the output voltage is applied in series with the input voltage through the feedback circuit. This is also knownas series-driven series- fed feedbacki.e., a series-series circuit.

The following figure shows the block diagram of current series feedback, by which it is evident that the feedback circuit is placed inseries with the output and also with the input.



Asthefeedbackcircuitisconnectedinserieswiththeoutputandthe inputaswell, both the output impedance and the input impedance are increased.

UNIT –V

OSCILLATORS:

Classification of oscillators, Barkhausen criterion, RC phase shift oscillator, Wein-bridge oscillator, LC oscillators- Hartley and Colpitts oscillator.

Oscillators:

An **oscillator** generates output without any ac input signal. An electronicoscillator is a circuit which converts dc energy into ac at a very high frequency. An amplifier with a positive feedback can be understood as an oscillator.

Amplifiervs.Oscillator

An**amplifier**increasesthesignalstrengthoftheinputsignalapplied,whereas an**oscillator**generatesa signalwithoutthat input signal,but it requiresdcforitsoperation. This is the main difference between an amplifier and anoscillator.

Take a look at the following illustration. It clearly shows how an amplifier takesenergyfrom d.c. power source and converts it into a.c. energy at signal frequency. An oscillator produces an oscillating a.c. signal on its own.



The frequency, waveform, and magnitude of a.c. power generated by an amplifier, is controlled by the a.c. signal voltage applied at the input, whereas those for an oscillator are controlled by the components inthecircuit itself, which means no external controlling voltage required.

Alternatorvs.Oscillator

An **alternator** is a mechanical device that produces sinusoidal waves without any input. This a.c. generating machine is used to generate frequencies up to 1000Hz. Theoutput frequency depends on the number of poles and the speed of rotation of the armature.

The following points highlight the differences between an alternator and an oscillator-

- Analternatorconvertsmechanicalenergytoa.c.energy,whereastheoscillator converts d.c. energy into a.c. energy.
- AnoscillatorcanproducehigherfrequenciesofseveralMHzwhereasanalternator cannot.
- Analternatorhasrotatingparts, whereas an electronic oscillator doesn't.
- Itiseasytochangethefrequencyofoscillationsinanoscillatorthaninan alternator.

Oscillatorscanalsobeconsidered as opposite to rectifiers that convert a.c. to a.c.

ClassificationofOscillators

Electronicoscillatorsareclassified mainly into the following two categories -

- Sinusoidal Oscillators The oscillators that produce an output having a sine waveformarecalled sinusoidalorharmonicoscillators. Suchoscillators canprovide output at frequencies ranging from 20 Hz to 1 GHz.
- Non-sinusoidalOscillators The oscillators that produce an output having a square, rectangular or saw-tooth waveform are called non-sinusoidal or relaxation oscillators. Such oscillators can provide output at frequencies ranging from 0 Hz to 20MHz.

SinusoidalOscillators

Sinusoidaloscillatorscanbeclassified in the following categories-

- Tuned Circuit Oscillators These oscillators use a tuned-circuit consisting of inductors (L) and capacitors (C) and are used to generate high-frequency signals. Thus they are also known as radio frequency R.F. oscillators. Such oscillators are Hartley, Colpitts, Clapp-oscillators etc.
- RC Oscillators There oscillators use resistors and capacitors and are used to generate low or audio-frequency signals. Thus they are also known as audiofrequency (A.F.) oscillators. Such oscillators are Phase –shift and Wein-bridge oscillators.
- Crystal Oscillators These oscillators use quartz crystals and are used to generate highly stabilized output signal with frequencies upto 10MHz. The Piezo oscillator is an example of a crystal oscillator.
- Negative-resistance Oscillator These oscillators use negative-resistance characteristic of the devices such as tunnel devices. A tuned diode oscillator is an example of a negative-resistance oscillator.

NatureofSinusoidalOscillations

Thenatureofoscillationsinasinusoidalwaveisgenerallyoftwotypes. Theyare **damped** and **undampedoscillations**.

DampedOscillations

Theelectricaloscillationswhoseamplitudegoesondecreasingwithtimearecalled as **Damped Oscillations**. The frequency of the damped oscillations may remain constant depending upon the circuit parameters.



Dampedoscillationsaregenerallyproducedbytheoscillatorycircuitsthatproducepower losses and doesn't compensate if required.
UndampedOscillations

The electrical oscillations whose amplitude remains constant with time are called as **UndampedOscillations**. The frequency of the undamped oscillations remains constant.



Undamped Oscillations

Undamped oscillations are generally produced by the oscillatory circuits that produce nopower losses andfollow compensation techniques if any power losses occur.

An amplifier with positive feedback produces its output to be in phase with the input and increases the strength of the signal. Positive feedback is also called as **degenerative feedback** or**direct feedback**. This kind of feedback makes a feedback amplifier, an oscillator.

The use of positive feedback results in a feedback amplifier having closed-loop gain greater than the open-loop gain. It results in **instability** and operates as an oscillatory circuit. An oscillatorycircuit provides aconstantlyvarying amplified outputsignalofany desired frequency.

TheBarkhausenCriterion

With the knowledge we have till now, we understood that a practical oscillator circuit consists of atank circuit, atransistor amplifier circuit and feedback circuit.so, let us now try to brushup the concept of feedback amplifiers, to derive the gain of the feedback amplifiers.

PrincipleofFeedbackAmplifier

A feedback amplifier generally consists of two parts. They are the **amplifier** and the **feedback circuit**. The feedback circuit usually consists of resistors. The concept of feedback amplifier can be understood from the following figure below.



From the above figure, the gain of the amplifier is represented as A. The gain of the amplifier is the ratio ofoutput voltage Vo to the input voltage V_i. The feedback network extracts avoltage $V_f = \beta V_o$ from the output V_o of the amplifier.

This voltage is added for positive feedback and subtracted for negative feedback, from the signal voltage V_s .

So, for a positive feedback,

 $V_i = V_s + V_f = V_s + \beta V_o$

The quantity $\beta = V_f / V_o$ is called as feedback ratio or feedback fraction.

 $The output V_{\circ} must be equal to the input voltage (V_{s} + \beta V_{\circ}) multiplied by the gain A of the amplifier.$

Hence,

(Vs+βVo)A=Vo

Or

AVs+AβVo=Vo

Or

 $AVs=Vo(1-A\beta)$

Therefore

$$\frac{V_o}{V_s} = \frac{A}{(1 - A\beta)}$$

 $Let A_f be the overall gain (gain with the feedback) of the amplifier. This is defined as the ratio of output voltage V_o to the applied signal voltage V_s, i.e.,$

$$\begin{array}{c} A_f \\ = V_o \\ \Psi_s \end{array}$$

from the above two equations, we can understand that, the equation of gain of the feedback amplifier ${}_{\!A}$ with positive feedback is given by

$$Af = \frac{1}{1 - A\beta}$$

Where $A\beta$ is the feedback factor or the loop gain.

If $A\beta=1$, $A_f=\infty$. Thus the gain becomes infinity, i.e., there is output without any input. In another words, the amplifier works as an Oscillator.

 $The condition A\beta = 1 is called as {\it BarkhausenCriterionofoscillations}. This is a very important factor to be always kept inmind, in the concept of Oscillators$

RC-Phase—shiftOscillators

PrincipleofPhase-shiftoscillators

We know that the output voltage of an RC circuit for a sinewave input leads the input voltage.ThephaseanglebywhichitleadsisdeterminedbythevalueofRCcomponentsused in the circuit. The following circuit diagram shows asingle section of an RC network.



The output voltage V₁' across the resistor R leads the input voltage applied inputV₁by some phase angle ϕ° . If Rwere reduced to zero, V₁'will lead the V₁ by 90° i.e., ϕ° =90°.

However, adjusting R to zero would be impracticable, because it would lead to no voltage across R. Therefore, in practice, R is varied to such a value that makes V_1' to lead V_1 by 60°. The following circuit diagram shows the three sections of the RC network.



 $\label{eq:Eachsectionproduces a phase shift of 60°. Consequently, atotal phase shift of 180° is produced,$ i.e., voltage V_2 leads the voltage V_1 by 180°.

Phase-shiftOscillatorCircuit

The oscillator circuit that produces a sine wave using a phase-shift network is called as a Phase-shift oscillator circuit. The constructional details and operation of a phase-shift oscillator circuit are as given below.

Construction

The phase-shift oscillator circuit consists of a single transistor amplifier section and a RC phase-shift network. The phase shift network in this circuit, consists of three RC sections. At the resonant frequency f_0 , the phase shift in each RC section is 60° so that the total phase shift produced by RC network is 180°.

ThefollowingcircuitdiagramshowsthearrangementofanRCphase-shift oscillator.



Thefrequencyofoscillationsisgivenby

$$f_o = \frac{1}{2\pi RC\sqrt{6}}$$

Where

$$R_1 = R_2 = R_3 = R$$

$$C_1 = C_2 = C_3 = C$$

Operation

The circuit when switched ON oscillates at the resonant frequency f_o . The output E_o of the amplifier is fed back toRC feedback network. This network produces a phase shift of 180°anda voltage E_i appears at its output. This voltage is applied to the transistor amplifier.

Thefeedbackappliedwillbe

m=Ei/Eo

The feedback is in correct phase, whereas the transistor amplifier, which is in CE configuration, produces a 180° phases hift. The phases hift produced by network and the transistor add to form a phase shift around the entire loop which is 360°.

Advantages

TheadvantagesofRCphaseshiftoscillatorareasfollows-

- Itdoesnotrequiretransformersorinductors.
- It can be used to produce very low frequencies.
- Thecircuitprovidesgoodfrequencystability.

Disadvantages

The disadvantages of RCphases hift oscillatorare as follows-

- Startingtheoscillationsisdifficultasthefeedbackissmall.
- Theoutputproducedissmall.

Another type of popular audio frequency oscillator is the Wien bridge oscillator circuit. This is mostly used because of its important features. This circuit is free from the **circuit fluctuations** and the **ambient temperature**.

Themain advantageofthisoscillatoristhatthefrequencycanbevariedin therangeof 10Hz toabout 1MHz whereas in RC oscillators, the frequency is not varied.

Wienbridge

oscillator

Construction

The circuit construction of Wien bridge oscillator can be explained as below. It is a two-stageamplifierwith RC bridge circuit. The bridge circuit has the arms R_1C_1 , R_3 , R_2C_2 and the tungsten lamp L_p. Resistance R₃ and the lamp L_p are used to stabilize the amplitude of the output.

The following circuit diagrams hows the arrangement of a Wienbridge oscillator.



The transistor T_1 serves as an oscillator and an amplifier while the other transistor T_2 serves as an inverter. The inverter operation provides a phase shift of 180°. This circuitprovides positive feedback through R_1C_1 , C_2R_2 to the transistor T_1 and negative feedback through the voltage divider to the input of transistor T_2 .

The frequency of oscillations is determined by the series element R_1C_1 and parallelelement R_2C_2 of the bridge.

$$f = \frac{1}{2\pi\sqrt{R_1C_1R_2C_2}}$$

 $IfR_1=R_2andC_1=C_2=C$

Then,

$$f=\frac{1}{2\pi RC}$$

Now, we can simplify the above circuit as follows-



The oscillator consists of two stages of RC coupled amplifier and a feedback network. The voltage across the parallel combination of R and C is fed to the input of amplifier 1. The net phase shift through the two amplifiers is zero.

The usual idea of connecting the output of amplifier 2 to amplifier 1 to provide signal regeneration for oscillator is not applicable here as the amplifier 1 will amplify signals over a wide range of frequencies and hence direct coupling would result inpoorfrequency stability. By adding Wienbridgefeedbacknetwork, the oscillator becomessensitive to aparticular frequency and hence frequency stability is achieved.

Operation

When the circuit is switched ON, the bridge circuit produces oscillations of the frequency stated above. The two transistors produce a total phase shift of 360° so that proper positive feedback is ensured. The negative feedback in the circuit ensures constant output. This is achievedby temperature sensitive tungstenlamp L_p. Its resistance increases with current.

If the amplitude of the output increases, more current is produced and more negative feedback is achieved. Due to this, the output would return to the original value. Whereas, if the output tends to decrease, reverse action would take place.

Advantages

Theadvantages of Wienbridge oscillator areas follows-

• Thecircuitprovidesgoodfrequencystability.

- Itprovidesconstantoutput.
- Theoperationofcircuitisquiteeasy.
- Theoverallgainishighbecause of two transistors.
- Thefrequencyofoscillationscanbechangedeasily.
- Theamplitudestabilityoftheoutputvoltagecanbemaintainedmoreaccurately,by replacing R₂ with a thermistor.

Disadvantages

ThedisadvantagesofWienbridgeoscillatorareas follows-

- Thecircuitcannotgenerateveryhighfrequencies.
- Twotransistorsandnumberofcomponentsarerequiredforthecircuitconstruction.

LCOscillators

An oscillatory circuit produces electrical oscillations of a desired frequency. They are also known as **tank circuits**.

A simple tank circuit comprises of an inductor L and a capacitor C both of which together determine the oscillatory frequency of the circuit.

To understand the concept of oscillatory circuit, let us consider the following circuit. The capacitor in this circuit is already charged using a dc source. In this situation, the upper plate of the capacitor has excess of electrons whereas the lower plate has deficit of electrons. The capacitor holds some electrostatic energy and there is avoltage across the capacitor.



When the switch **S** is closed, the capacitor discharges and the current flows through the inductor. Due to the inductive effect, the current build supslowly towards a maximum value. Once the capacitor discharges completely, the magnetic field around the coilis maximum.



Now, let us move on to the next stage. Once the capacitor is discharged completely, the magnetic field begins to collapse and produces a counter EMF according to Lenz's law. The capacitor is now charged with positive charge on the upper plate and negative charge on the lowerplate.



Oncethecapacitorisfullycharged, itstartstodischargetobuildupamagnetic field around th e coil, as shown in the following circuit diagram.



This continuation of charging and discharging results in alternating motion of electrons or an **oscillatory current**. The interchange of energy between L and C produce continuous **oscillations**.

In an ideal circuit, where there are no losses, the oscillations would continue indefinitely. In a practical tank circuit, there occur losses such as **resistive** and **radiation losses** in the coil and **dielectric losses** in the capacitor. These losses result in damped oscillations.

FrequencyofOscillations

The frequency of the oscillations produced by the tank circuit are determined by the components of the tank circuit, **the L** and **the C**. The actual frequency of oscillations is the **resonantfrequency** (ornatural frequency) of the tank circuit which is given by

$$f_r = \frac{1}{2\pi L \sqrt{C}}$$

Capacitanceofthecapacitor

The frequency of oscillation f_0 is inversely proportional to the square rootof the capacitance of a capacitor. So, if the value of the capacitor used is large, the charge and discharge time periods will be large. Hence the frequency will be lower.

Mathematically, the frequency,

$$f_0 \propto^1 \frac{1}{\sqrt{C}}$$

Self-Inductance of the coil

The frequency of the oscillation f_0 is proportional to the square root of the self-inductance of the coil. If the value of the inductance is large, the opposition to change of current flow is greater and hence the time required to complete each cycle will be longer, which means time period will be longer and frequency will be lower.

Mathematically, the frequency,

$$f_{o} \propto \frac{1}{\sqrt{L}}$$

Combiningboththeabove
equations,
$$f_{o} \propto \frac{1}{\sqrt{LC}}$$

$$f_{o} = \frac{1}{2\pi I/C}$$

The above equation, though indicates the output frequency, matchesthe**naturalfrequency** or **resonance frequency** of the tank circuit.

An Oscillator circuit is a complete set of all the parts of circuit which helps to produce the oscillations. These oscillations shouldsustainand shouldbe Undampedas just discussedbefore. Let us try to analyze a practical Oscillator circuit to have a better understanding on how an Oscillator circuit works.

PracticalOscillatorCircuit

A Practical Oscillator circuit consists of a tank circuit, a transistor amplifier, and a feedback circuit. The following circuit diagram shows the arrangement of a practical oscillator.



Letusnowdiscussthepartsofthispracticaloscillatorcircuit.

Tank Circuit – The tank circuit consists of an inductance L connected in parallel with capacitor **C**. The values of these two components determine the frequency of the oscillator circuit and hence this is called as **Frequency determining circuit**.

- Transistor Amplifier The output of the tank circuit is connected to the amplifier circuit so that the oscillations produced by the tank circuit are amplifiedhere. Hence the output of these oscillations are increased by the amplifier.
- FeedbackCircuit Thefunction of feedbackcircuitistotransfer apartofthe output energy to LC circuit in proper phase. This feedback is positive in oscillators while negative inamplifiers.

FrequencyStabilityofanOscillator

The frequency stability of an oscillator is a measure of its ability to maintain a constant frequency, over a long time interval. When operated over a longer period of time, the oscillator frequency may have a drift from the previously setvalue either by increasing orby decreasing.

The change in oscillator frequency may arised ue to the following factors -

- OperatingpointoftheactivedevicesuchasBJTorFETusedshouldlieinthelinear region of the amplifier. Its deviation willaffect the oscillatorfrequency.
- Thetemperaturedependencyoftheperformanceofcircuitcomponentsaffectthe oscillator frequency.
- Thechangesind.c.supplyvoltageappliedtotheactivedevice,shifttheoscillator frequency. This can be avoided if a regulated powersupply isused.
- Achangeinoutput loadmaycauseachangeintheQ-factorofthetank circuit, thereby causing a change in oscillator output frequency.
- Thepresenceofinterelementcapacitancesandstraycapacitancesaffect the oscillator output frequency and thus frequency stability.

Tuned circuit oscillators are the circuits that produce oscillations with the help of tuning circuits. The tuning circuits consists of an inductance L and a capacitor C. These are also known as **LC oscillators, resonant circuit oscillators** or **tank circuit oscillators**.

The tuned circuit oscillators are used to produce an output with frequencies ranging from 1 MHz to 500 MHz Hence these are also known as **R.F. Oscillators**. A BJT or a FET is used as an amplifierwithtunedcircuit oscillators. WithanamplifierandanLC tank circuit,we canfeedback a signalwith right amplitude and phase to maintain oscillations.

TypesofTunedCircuitOscillators

Most of the oscillators used in radio transmitters and receivers are of LC oscillators type. Depending upon the way the feedback is used in the circuit, the LC oscillators are divided as the following types.

- HartleyOscillator-Itusesinductivefeedback.
- ColpittsOscillator-Itusescapacitivefeedback.
- ClappOscillator-Itusescapacitivefeedback.

HartleyOscillator

A very popular **local oscillator** circuit that is mostly used in **radio receivers** is the **Hartley Oscillator** circuit. The constructional details and operation of a Hartley oscillator areas discussed below.

Construction

In the circuit diagram of a Hartley oscillator shown below, the resistors R_1 , R_2 and R_e provide necessary bias condition for the circuit. The capacitor C_e provides a.c. ground thereby providing any signal degeneration. This also provides temperature stabilization.

The capacitors C_c and C_b are employed to block d.c. and to provide an a.c. path. The radio frequency choke (R.F.C) offers very high impedance to high frequency currents which means it shorts for d.c. and opens for a.c. Hence it provides d.c. load for collector and keeps a.c. currents out of d.c. supply source

TankCircuit

The frequency determining network is a parallel resonant circuit which consists of the inductors L_1 and L_2 along with avariable capacitor C. The junction of L_1 and L_2 are earthed. The coil L_1 has its one end connected to base via C_c and the other to emitter via C_e . So, L_2 is in the output circuit. Both the coils L_1 and L_2 are inductively coupled and together form an **Auto-transformer**.

ThefollowingcircuitdiagramshowsthearrangementofaHartleyoscillator.Thetank circuit is **shuntfed** in this circuit. It canalso be a **series-fed**.



Operation

When the collector supply is given, a transient current is produced in the oscillatory or tank circuit. The oscillatory current in the tank circuit produces a.c. voltage across L₁.

The **auto-transformer** made by the inductive coupling of L_1 and L_2 helps in determining the frequency and establishes the feedback.AstheCEconfiguredtransistorprovides180°phase shift, another 180° phase shift is provided by the transformer, which makes 360° phase shift between the input and outputvoltages.

This makes the feedback positive which is essential for the condition of oscillations. When the **loop gain** $|\beta A|$ of the amplifier is greater than one, oscillations are sustained in the circuit.

Frequency

The equation for frequency of Hartley oscillator is given as

$$f = \frac{1}{2\pi\sqrt{L_TC}}$$

 $L_T = L_1 + L_2 + 2M$

Here, L_T is the total cumulatively coupled inductance; L₁ and L₂ represent inductances of 1st and 2nd coils; and **M** represents mutual inductance.

 $\label{eq:mutualinductance} Mutual inductance is calculated when two windings are considered.$

Advantages

TheadvantagesofHartleyoscillatorare

- Insteadofusinga largetransformer, asinglecoil can be used as an autotransformer.
- Frequencycanbevariedbyemployingeitheravariablecapacitororavariable inductor.
- Lessnumberofcomponentsaresufficient.
- The amplitude of the output remains constant over a fixed frequency range.

Disadvantages

The disadvantages of Hartley oscillatorare

- Itcannotbea lowfrequencyoscillator.
- Harmonicdistortionsarepresent.

Applications

 $\\The applications of {\sf Hartley} oscillator are$

- It is used to produce a sinewaye of desired frequency.
- Mostlyusedasalocaloscillatorinradioreceivers.
- ItisalsousedasR.F.Oscillator.

Colpittsoscillator

AColpitts oscillatorlooks just liketheHartley oscillatorbut theinductors and capacitors are replaced with each other in the tank circuit. The constructional details and operation of a colpitts oscillator are as discussed below.

Construction

 $\label{eq:letusfirst} Letus first take a look at the circuit diagram of a Colpitts oscillator.$



The resistors R_1 , R_2 and R_e providencessary bias condition for the circuit. The capacitor C_e provides a.c. ground thereby providing any signal degeneration. This also provides temperature stabilization.

The capacitors C_c and C_b are employed to block d.c. and to provide an a.c. path. The radio frequency choke (R.F.C) offers very high impedance to high frequency currents which means it shorts for d.c. and opens fora.c. Hence it provides d.c. load forcollector andkeeps a.c. currents out of d.c. supply source.

TankCircuit

The frequency determining network is a parallel resonant circuit which consists of variable capacitors C_1 and C_2 along with an inductor L. The junction of C_1 and C_2 are earthed. The capacitor C_1 has its one end connected to base via C_c and the other to emitter via C_e . the voltage developed across C_1 provides the regenerative feedback required for the sustained oscillations.

Operation

When the collector supplyis given, a transient current is produced in the oscillatory or tank circuit. The oscillatory current in the tank circuit produces a.c. voltage across C₁ which are

applied to the baseemitter junction and appear in the amplified form in the collector circuit and supply losses to the tank circuit.

If terminal 1 is at positive potential with respect to terminal 3 at any instant, then terminal 2 will be at negative potential with respect to 3 at that instant because terminal 3 is grounded. Therefore, points 1 and 2 are out of phase by 180°.

AstheCEconfiguredtransistorprovides 180° phaseshift, itmakes 360° phaseshift between the input and output voltages. Hence, feedback is properly phased to produce continuous Undamped oscillations. When the **loop gain** $|\beta A|$ of the amplifier is greater than one, oscillations are sustained in the circuit.

Frequency

The equation for frequency of Colpitts oscillator is given as

$$f = \frac{1}{2\pi\sqrt{LC_T}}$$

 $C_{T} is the total capacitance \ of C_{1} and C_{2} connected inseries.$

$$\frac{1}{C_T} = \frac{1}{C_1} + \frac{1}{C_2}$$
$$C_T = \frac{C_1 \times C_2}{C_1 + C_2}$$

Advantages

TheadvantagesofColpittsoscillatorareasfollows-

- Colpittsoscillatorcangeneratesinusoidalsignalsofveryhighfrequencies.
- Itcanwithstandhighandlowtemperatures.
- Thefrequencystabilityishigh.
- Frequencycanbevariedbyusingboththevariablecapacitors.
- Lessnumberofcomponentsaresufficient.
- The amplitude of the output remains constant over a fixed frequency range.

The Colpitts oscillator is designed to eliminate the disadvantages of Hartley oscillator and is known to have no specific disadvantages. Hence there are many applications of a colpitts oscillator. TheoperationofClapposcillatorcircuitis inthesamewayasthatofColpittsoscillator.Thefrequency of oscillator is given by the relation, $2\pi\sqrt{L}$. C

Where
$$\frac{1}{\frac{1}{C_1}+\frac{1}{C_2}+\frac{1}{C_3}}$$

Usually, the value of C_3 is much smaller than C_1 and C_2 . As a result of this, C is approximately equal to C_3 . Therefore, the frequency of oscillation,

$$_{o} = \frac{1}{2\pi\sqrt{L. C_{3}}}$$

It is understood that the Clapp oscillator is similar to the Colpitts oscillator, however they differinthe way the inductances and capacitances are arranged. The frequency stability though is good, can be variable in a Clapp oscillator.

A Clapp oscillator is sometimes preferred over a Colpitts oscillator for constructinga variable frequency oscillator. The Clapp oscillators are used in receiver tuning circuits as a frequency oscillator.

One of the important features of an oscillator is that the feedback energy applied should be in correct phase to the tank circuit. The oscillator circuits discussed so farhasemployed inductor(L) and capacitor (C) combination, in the tank circuit or frequency determining circuit.

We have observed that the LC combination in oscillators provide 180° phase shift and transistor in CE configuration provide180° phase shift to make a total of 360° phase shift sothat it would make a zero difference in phase.

DrawbacksofLCcircuits

Though they have few applications, the LC circuits have few drawbacks such as

- Frequencyinstability
- Waveformispoor
- Cannotbeusedforlowfrequencies
- Inductorsarebulkyandexpensive

Whenever an oscillator is under continuous operation, its **frequency stability** gets affected. There occur changes in its frequency. The main factors that affect the frequency of an oscillatorare

- Powersupplyvariations
- Changesintemperature
- Changesinloadoroutputresistance

In RC and LC oscillators the values of resistance, capacitance and inductance vary with temperature and hence the frequency gets affected. In order to avoid this problem, the piezo electric crystals are being used in oscillators.